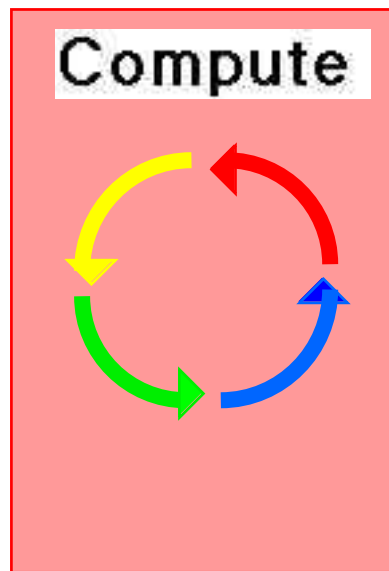


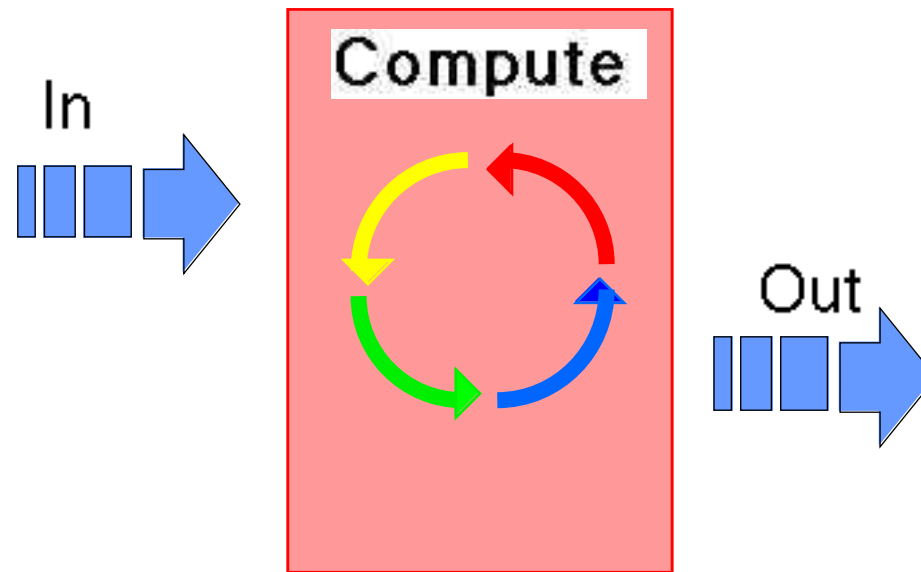
# EG2069: Part 1

## Introduction to Computers



Gorry Fairhurst

Dept of Engineering  
University of Aberdeen  
(c) 2000.



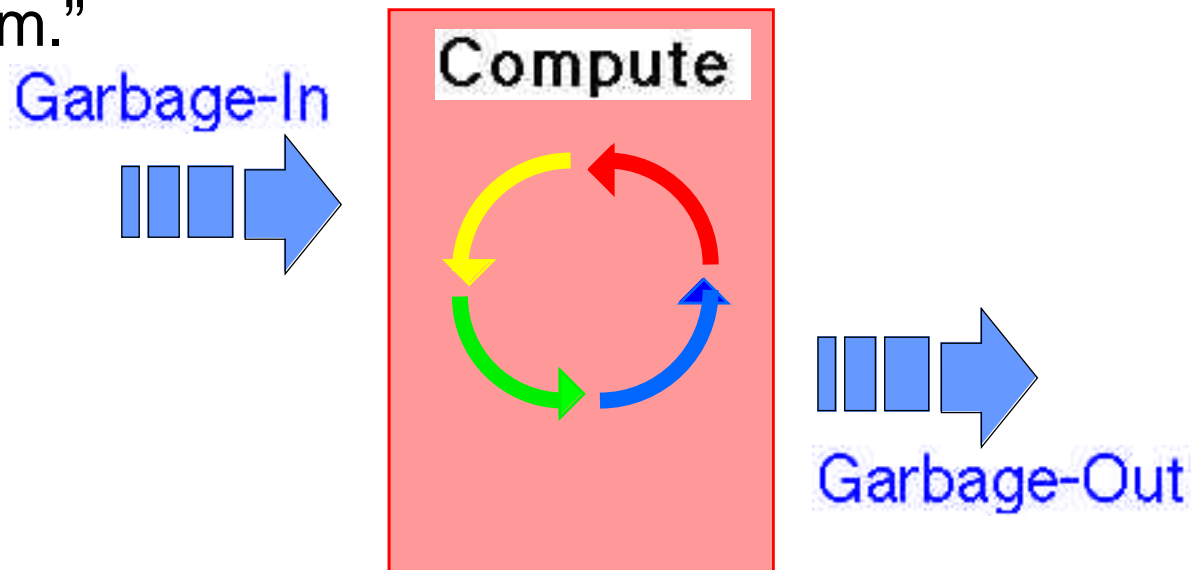
What is a computer?

# Definition of "Computer"

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*No fixed definition...*

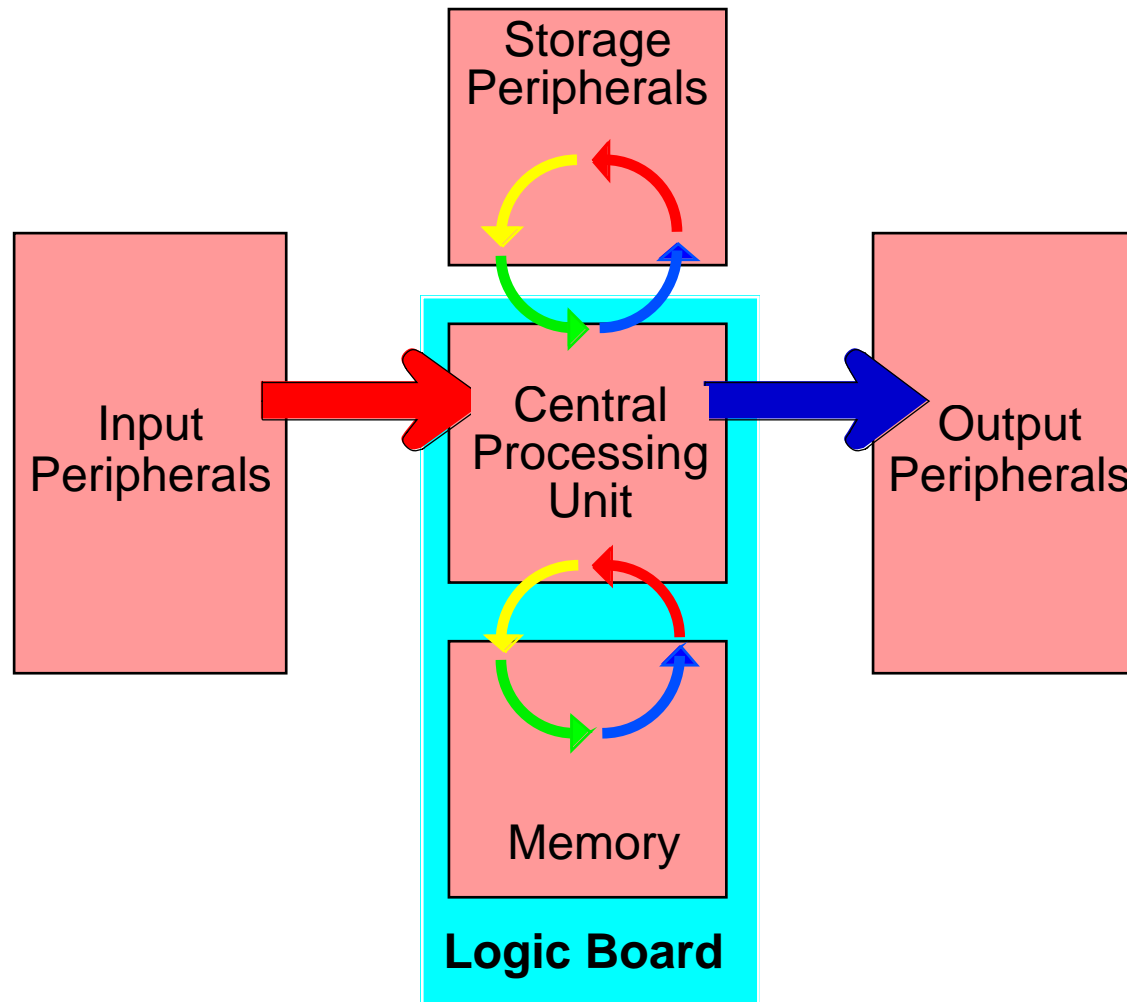
“A computer is a machine which can accept data, process the data and supply the results. The term is used for any computing device that operates according to a stored program.”



The computer is only useful with a **valid program** and **correct data**

# A Computer

Gorry Fairhurst



# Peripheral Devices

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## Input Devices

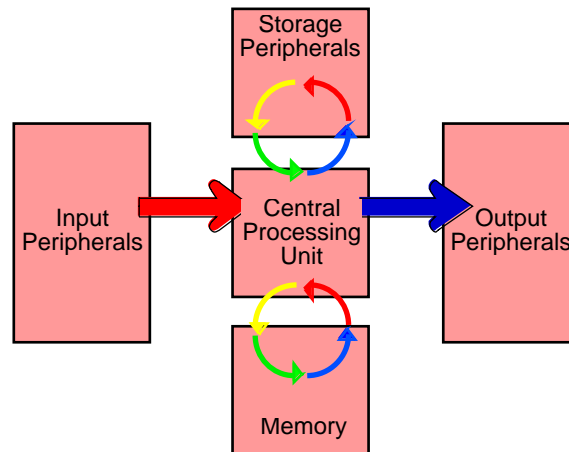
Scanner  
Optical Character Recognition  
Mouse  
Keyboard  
Microphone  
Bar Code Reader  
CD /CD-R  
DVD/DVD-ROM  
EPROM  
Modem

## Storage Devices

Magnetic Tape  
Magnetic Disks  
Magneto-Optical  
Discs  
CD-RW  
DVD-RAM  
Flash Card

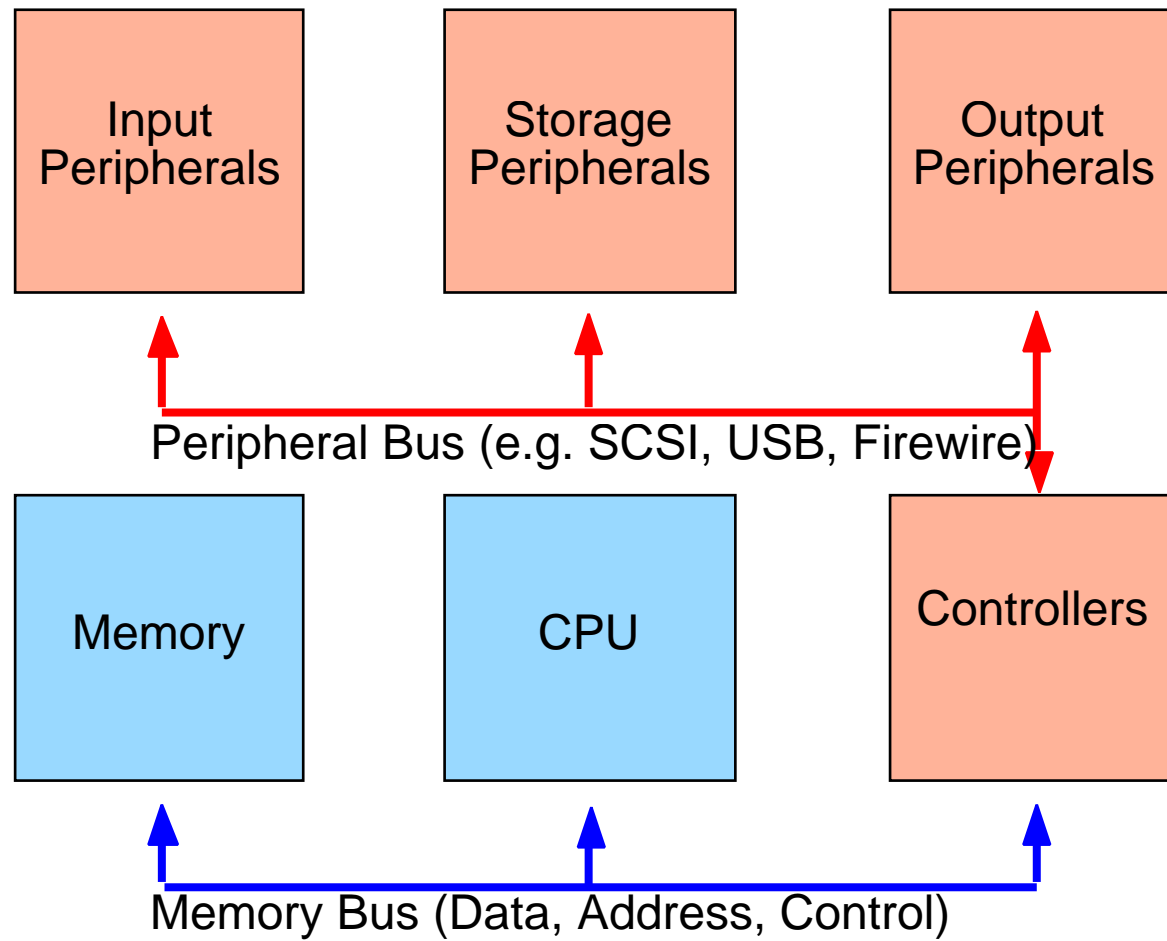
## Output Devices

Printer  
Plotter  
Punched Paper Tape  
CD-R  
DVD-ROM  
EPROM  
Modem

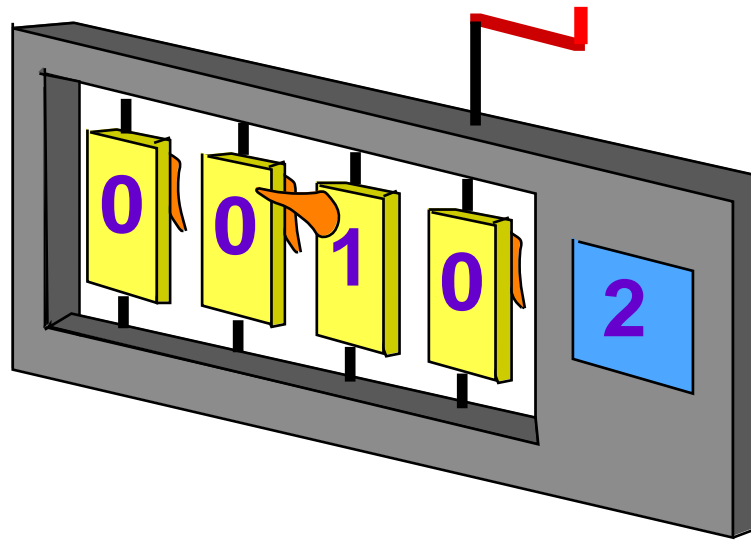


# Computer Busses

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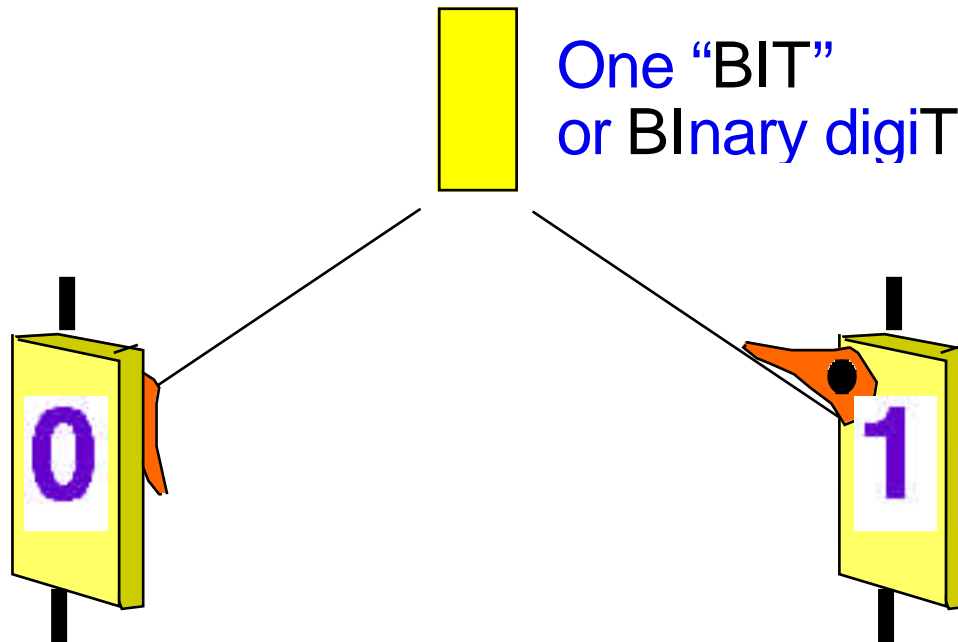
# Binary Numbers



# *Definition of a BIT*

---

Gorry Fairhurst



A bit can take only one of two values:

It is always either 0 or 1



# Nybbles, Bytes and Words

Gorry Fairhurst

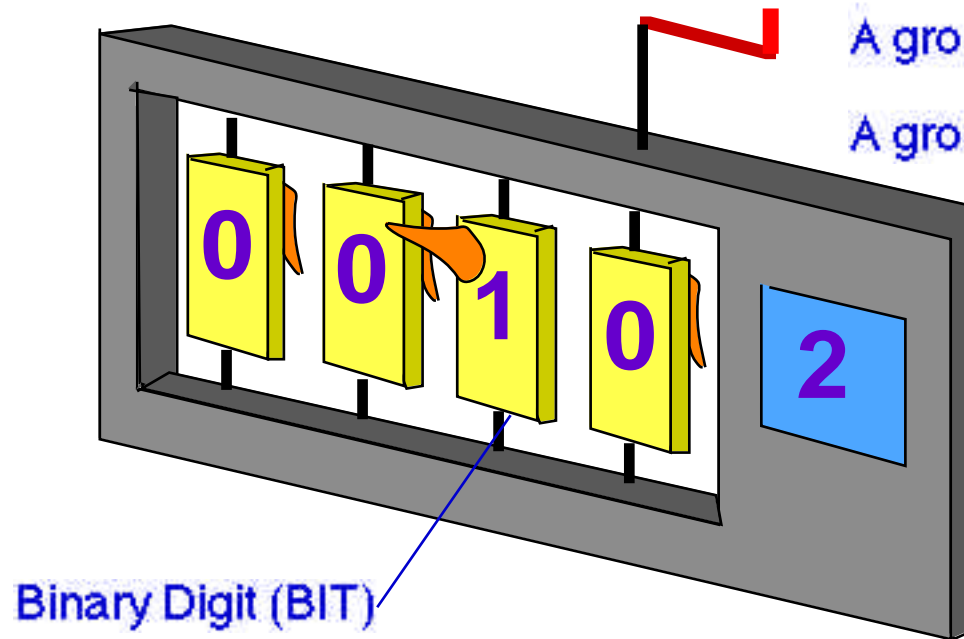
A single bit is not very useful

Bits are grouped together to form groups

A group of 4 bits = Nibble

A group of 8 bits = Byte

A group of bytes = Word



# Binary to Decimal

Gorry Fairhurst

Convert by adding weights of digits

e.g. consider the binary number 1010

$$\begin{aligned}1010 &= 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 \\ &= 8 + 2 \\ &= 10.\end{aligned}$$

The same process as in decimal

$$\text{e.g. } 305 = 3 \times 10^2 + 0 \times 10^1 + 5 \times 10^0$$

N.B. 100 in decimal = one hundred  
100 in binary = four

Dec.	Binary
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111

# Decimal to Binary

Gorry Fairhurst

Use repeated division by 2,  
and record the remainders

e.g. convert 12 in decimal to binary

$$\begin{array}{rcl} 12 / 2 & = & 6 \quad \text{rem } 0 \\ 6 / 2 & = & 3 \quad \text{rem } 0 \\ 3 / 2 & = & 1 \quad \text{rem } 1 \\ 1 / 2 & = & 0 \quad \text{rem } 1 \end{array}$$



Reading the remainders upwards:  
12 is 1100 in binary

You can check by converting it back:

$$\begin{aligned} 1100 &= 1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 0 \times 2^0 \\ &= 8 + 4 = 12 \end{aligned}$$

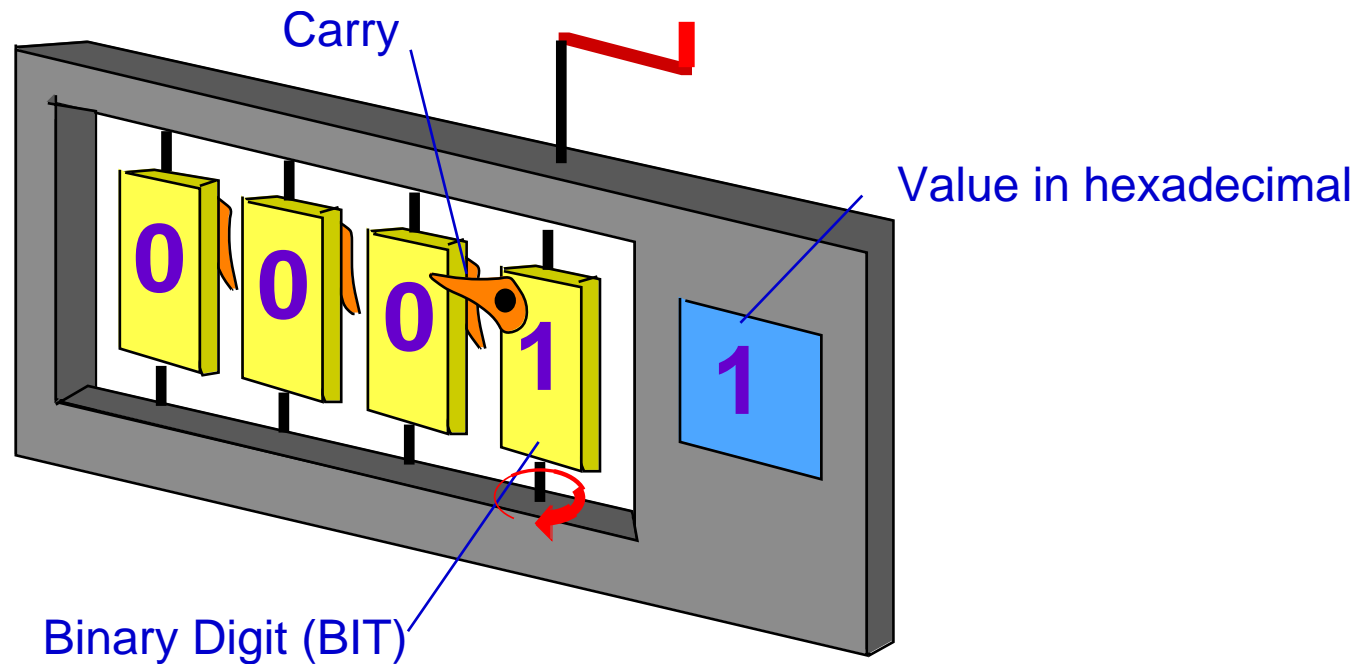
Dec.	Binary
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111

# Model of a Register

Gorry Fairhurst

Computers hold binary values in a “register”

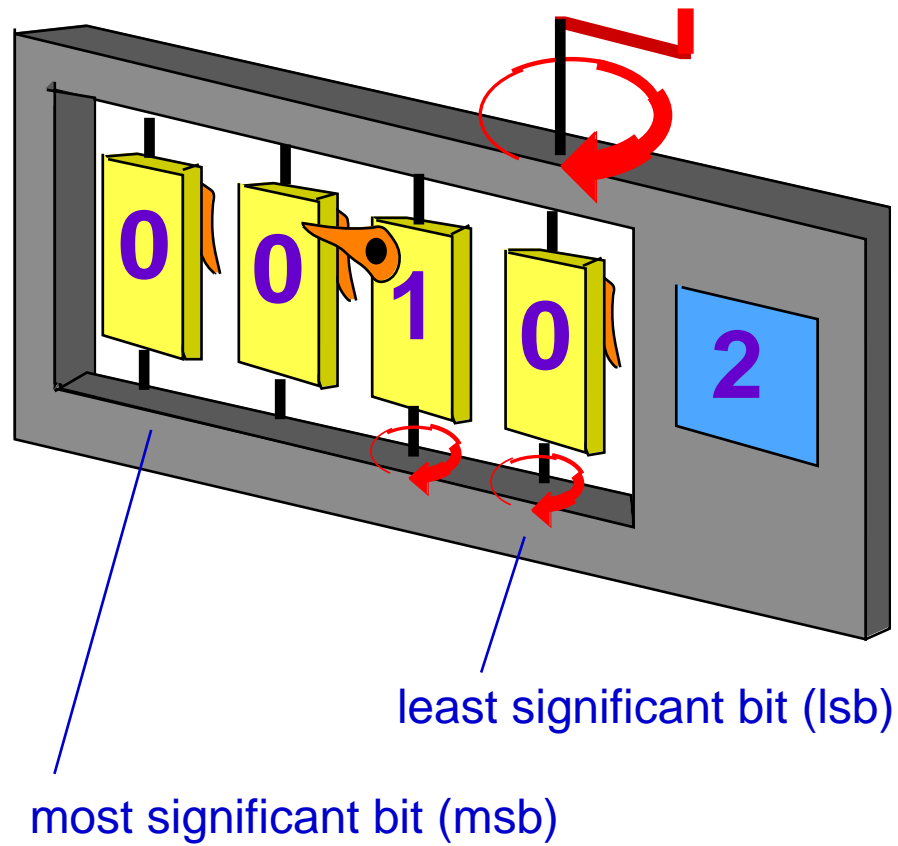
Consider the process of *incrementing* a register  
(adding one to the value stored in the register)



# Incrementing the Model Register

Gorry Fairhurst

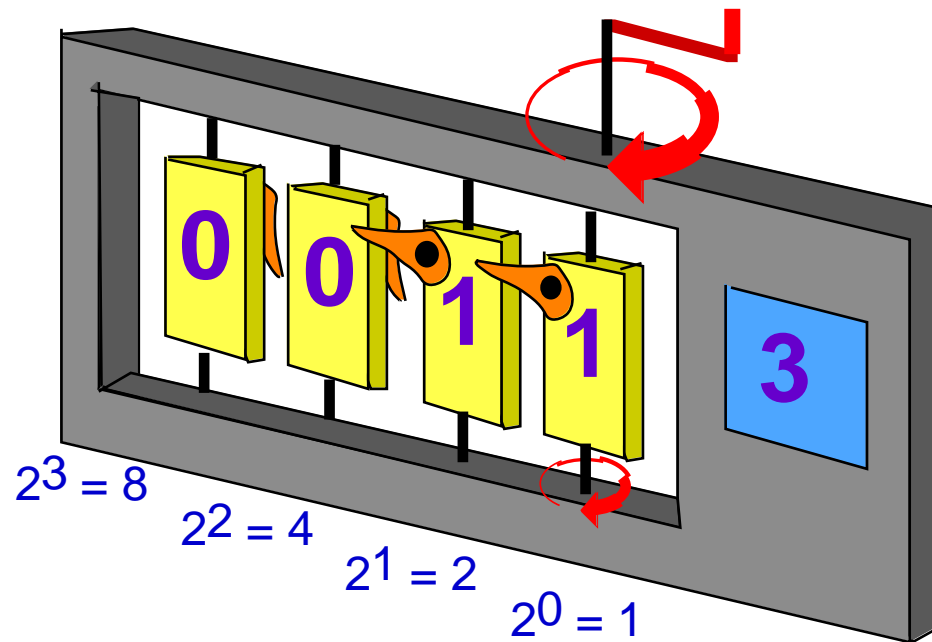
*register ++*



# Incrementing the Model Register

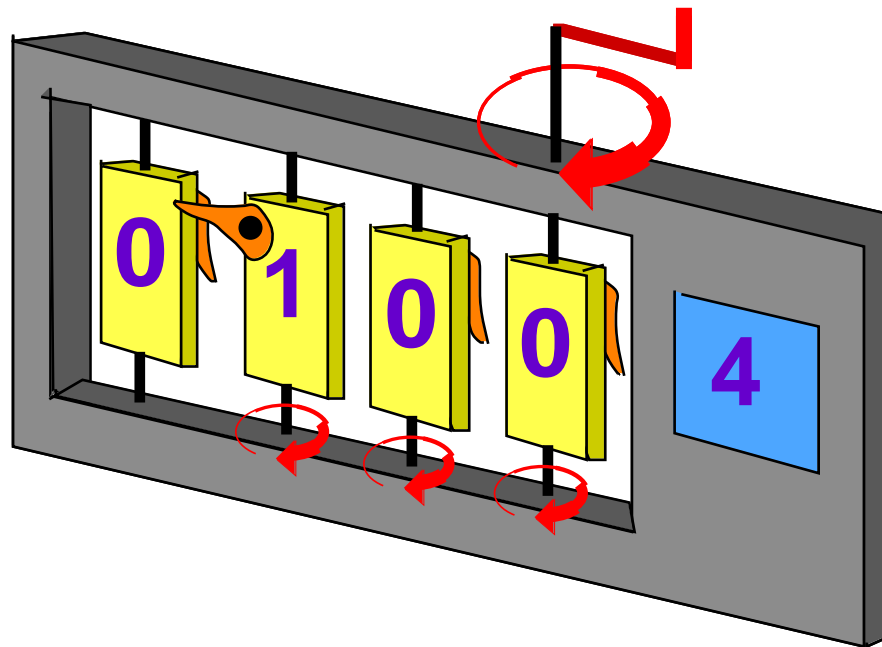
Gorry Fairhurst

*register ++*



# Incrementing the Model Register

Gorry Fairhurst



*register ++*

To add  $n$ , turn handle “ $n$ ” times.

*N.B. Real registers don't use handles!!!  
They use logic gates - but they do generate carries between digits*

# Binary Addition

Gorry Fairhurst

Adding single digits

$$\begin{array}{r} 0 \\ + 0 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 0 \\ + 1 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 1 \\ + 0 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 1 \\ + 1 \\ \hline 10 \end{array}$$

Adding binary numbers

$$\begin{array}{r} 010 \\ + 101 \\ \hline 111 \end{array}$$

$$\begin{array}{r} 110 \\ + 101 \\ \hline 1011 \\ 1 \end{array}$$

$$\begin{array}{r} 101 \\ + 011 \\ \hline 1000 \\ 111 \end{array}$$

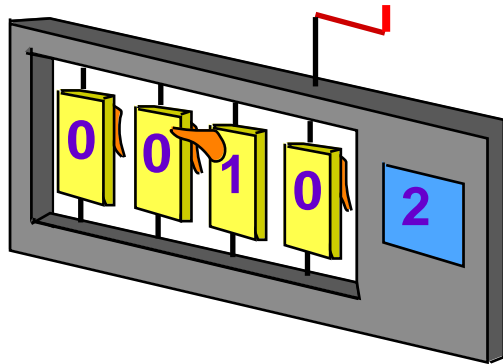
Carry





## Groups of 4 Bits

Gorry Fairhurst



In general a group of  $n$  bits  
may represent a set of  $2^n$  values

i.e. digits  $\{0, 1, 2, \dots, (2^n - 1)\}$

For 4 bits,  $n=4$  therefore  $2^4$  or 16 values

Digits 0..15  $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15\}$

It's not convenient to use two symbols for one digit!!!

So we normally use letters for digits greater than 9

Hence:  $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F\}$

# Converting Hexadecimal to Binary

Gorry Fairhurst

Numbers represented by digits {0..F}  
use base 16, or **hexadecimal**

Each hexadecimal digit may be  
represented by 4 bit.

To convert a hexadecimal number  
to binary convert each digit:

0x01FF = 0000 0001 1111 1111

Similarly:

1111 1111 0000 0000 =0xF0

*N.B. To recognise hex numbers  
we usually write "0x" before them!*

Dec.	Hex.	Binary
0	0x0	0000
1	0x1	0001
2	0x2	0010
3	0x3	0011
4	0x4	0100
5	0x5	0101
6	0x6	0110
7	0x7	0111
8	0x8	1000
9	0x9	1001
10	0xA	1010
11	0xB	1011
12	0xC	1100
13	0xD	1101
14	0xE	1110
15	0xF	1111

# Converting Hexadecimal to Decimal

Gorry Fairhurst

Convert Hex to decimal by adding weights of digits

$$\begin{aligned} 0x1C7 &= 1 \times 16^2 + C \times 16^1 + 7 \times 16^0 \\ &= 1 \times 256 + 12 \times 16 + 7 \\ &= 455. \end{aligned}$$

Convert Decimal to Hexadecimal by repeated division by 16.  
e.g. convert 456 to hex

$$\begin{array}{llll} 456 / 16 & = 28 & \text{rem } 8 & (0x8) \\ 28 / 16 & = 1 & \text{rem } 12 & (0xC) \\ 1 / 16 & = 0 & \text{rem } 1 & (0x1) \end{array}$$



Dec.	Hex.
0	0x0
1	0x1
2	0x2
3	0x3
4	0x4
5	0x5
6	0x6
7	0x7
8	0x8
9	0x9
10	0xA
11	0xB
12	0xC
13	0xD
14	0xE
15	0xF

Reading the remainders upwards:  
456 is 0x1C8 in hexadecimal

## More Examples

Gorry Fairhurst

### Decimal to Hexadecimal

Converting 53241 decimal to hexadecimal:

53241	÷16	=3327	R 9	(0x9)	msb
3327	÷16	= 207	R 15	10 (0xF)	↑
207	÷16	= 12	R 15	10 (0xF)	lsb
12	÷16	= 0	R 12	10 (0xC)	

53241 = 0x00CFF9

Convention that positive numbers start with 0x0

### Hexadecimal to Decimal

Converting 0x00CFF9 to decimal:

$$\begin{aligned} &= (9 \times 16^3) + (15 \times 16^2) + (15 \times 16^1) + (12 \times 16^0) \\ &= 53241 \end{aligned}$$

Value of digit

Position of digit

# Hexadecimal Addition

Gorry Fairhurst

$$\begin{array}{r} 20 \\ +5 \\ \hline =25 \end{array} \quad \begin{array}{r} 0x14 \\ +0x05 \\ \hline =0x19 \end{array} \quad \begin{array}{r} 0001\ 0100 \\ +0000\ 0101 \\ \hline =0001\ 1001 \end{array}$$

a b c	S	C
0 0 0	0	0
0 0 1	1	0
0 1 0	1	0
0 1 1	0	1
1 0 0	1	0
1 0 1	0	1
1 1 0	0	1
1 1 1	1	1

**3 bit binary adder**

0 + 1 = 1

0 + 0 = 0

1 + 1 = 0, c

0 + 0 + c = 1

0 + 1 = 1

N.B.

Sum = 1 if there are an odd number of 1's

Carry = 1 if there are two or more 1's

# Number Systems

---

Gorry Fairhurst

## Binary

2 values per digit {0,1}

e.g.  $10100 = 1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 0 \times 2^0$

## Decimal

10 values per digit {0,1,2,3,4,5,6,7,8,9}

e.g.  $20 = 2 \times 10^1 + 0 \times 10^0$

## Hexadecimal

16 values per digit {0,1,2,3,4,5,6,7,8,9,A,B,C,D,E,F}

e.g.  $14 = 1 \times 16^1 + 4 \times 16^0$

# Hexadecimal Signed Numbers

Gorry Fairhurst

## 1's Complement (bit-wise inversion)

int x  
x = ~x  
e.g.

int's are normally 4 r1 (or 8 nibbles)

Examples using a 32 bit register (8 hexadecimal digits)

20 = 0x00000014

msb = 0 for positive number  
msb = 1 for negative number.

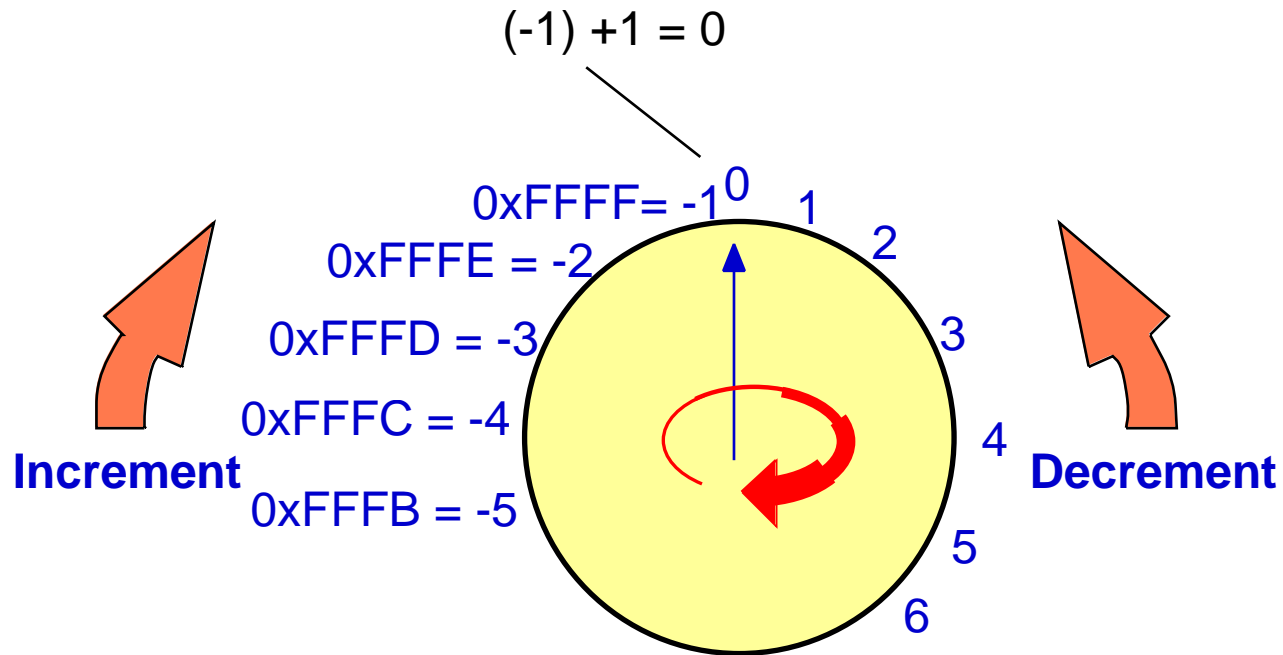
-20 = 0xFFFFFEB

0x means the number is in hexadecimal

Note that the *size* of variable determines how many digits!

# Hexadecimal Signed Numbers

Gorry Fairhurst





# Subtraction

Gorry Fairhurst

Subtraction is **difficult!**

Easier to **negate** a value in 2's complement and then **add**

20	0x14	0001 0100	0001 0100	-5 as a
-5	- 0x05	- 0000 0101	+1111 1011	byte
<hr/>	<hr/>	<hr/>	<hr/>	
=15	=0x0F	=0000 1111	= 0000 11 11	

A carry is generated and ignored at the msb

# Hexadecimal Signed Numbers

Gorry Fairhurst

## 2's Complement (true negation)

int x  
 $x = (\sim x) + 1$

Examples using a 32 bit register  
(8 hexadecimal digits)

e.g.

20 = 0x00000014

Sufficient to add 1 or 2 zeros  
before the first non-zero digit.

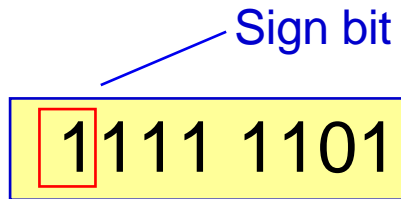
-20 = 0xFFFFFEC

More care is needed to get the size  
correct for negative numbers

# Signed and Unsigned Numbers

---

Gorry Fairhurst



The binary value “1111 1101” has the msb set, it may therefore be interpreted as either:

The *unsigned char* 0x00FD (+253)

or

The *signed char* 2's complement number 0xFD (-3)

*N.B.*

*In C the size of the type “char” is one byte  
It is important to know the **type** of the number  
to determine the value when the msb is set to 1.*

# Size of Variables

---

Gorry Fairhurst

char (8 bits)

0111 1101
-----------

short int (16 bits)

0000 0000	0111 1101
-----------	-----------

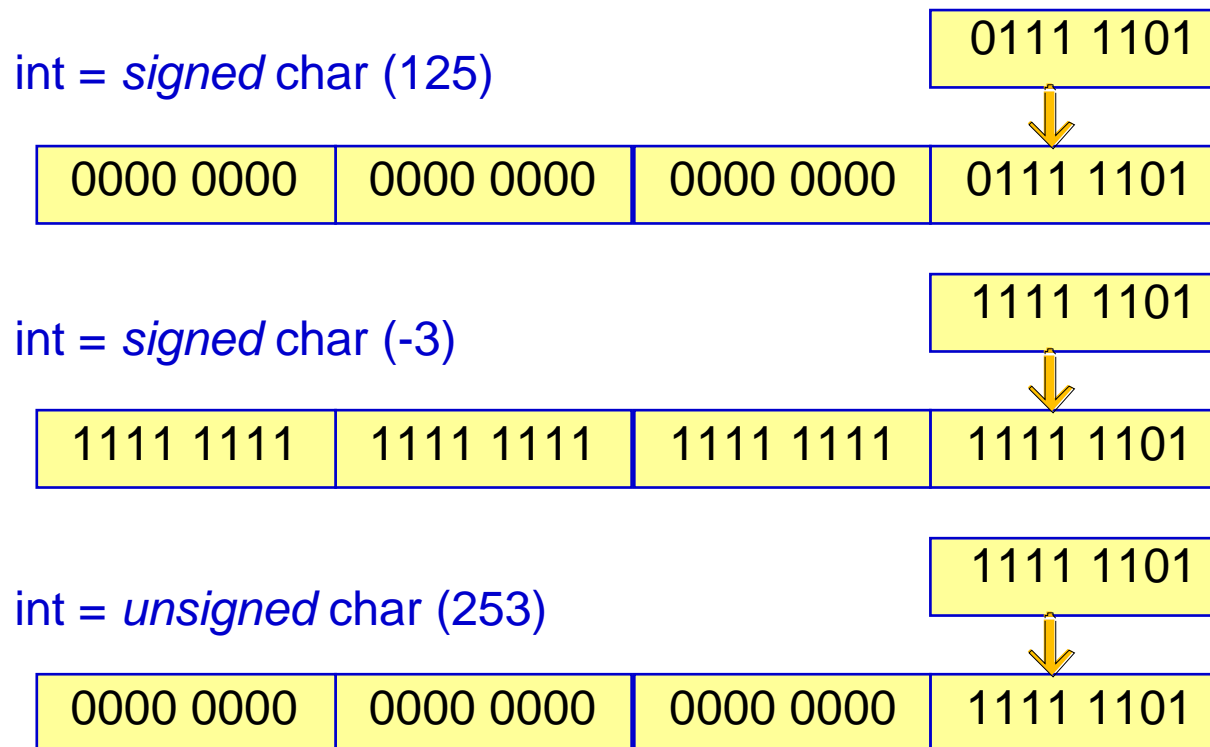
int (32 bits)

0000 0000	0000 0000	0000 0000	0111 1101
-----------	-----------	-----------	-----------

*N.B. The assembler (or compiler) must determine the size of each variable to use the correct instruction*

# Type Conversion

Gorry Fairhurst



*N.B. For signed values, the sign must be **extended***

## Multiplication by 2

---

Gorry Fairhurst

Multiplication by 2 implies adding a 0 to a binary number

e.g. consider the binary number 1010 (10 in decimal) x 2

$$1010 \times 2 = 10100$$

$$= 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0$$

$$= 20 \text{ (decimal)}$$

This is a **shift** operation, each digit is **shifted left**.

The same process as in decimal!

In the C programming language we write

a shift right n places as  $\ll n$ , meaning multiply by  $2^n$

Hence  $0x2 \ll 1 = 0x4$ ,  $0x1 \ll 2 = 0x4$ .

Use **long multiplication** to multiply by other values

## Division by 2

---

Gorry Fairhurst

Division by 2 implies deleting a digit from a binary number

e.g. consider the binary number 1010 (10 in decimal) / 2

$$\begin{aligned} 1010 / 2 &= 101 \\ &= 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 \\ &= 5 \text{ (decimal)} \end{aligned}$$

This is a ***shift*** operation, each digit is ***shifted right***.

The same process as in decimal!

In the C programming language we write

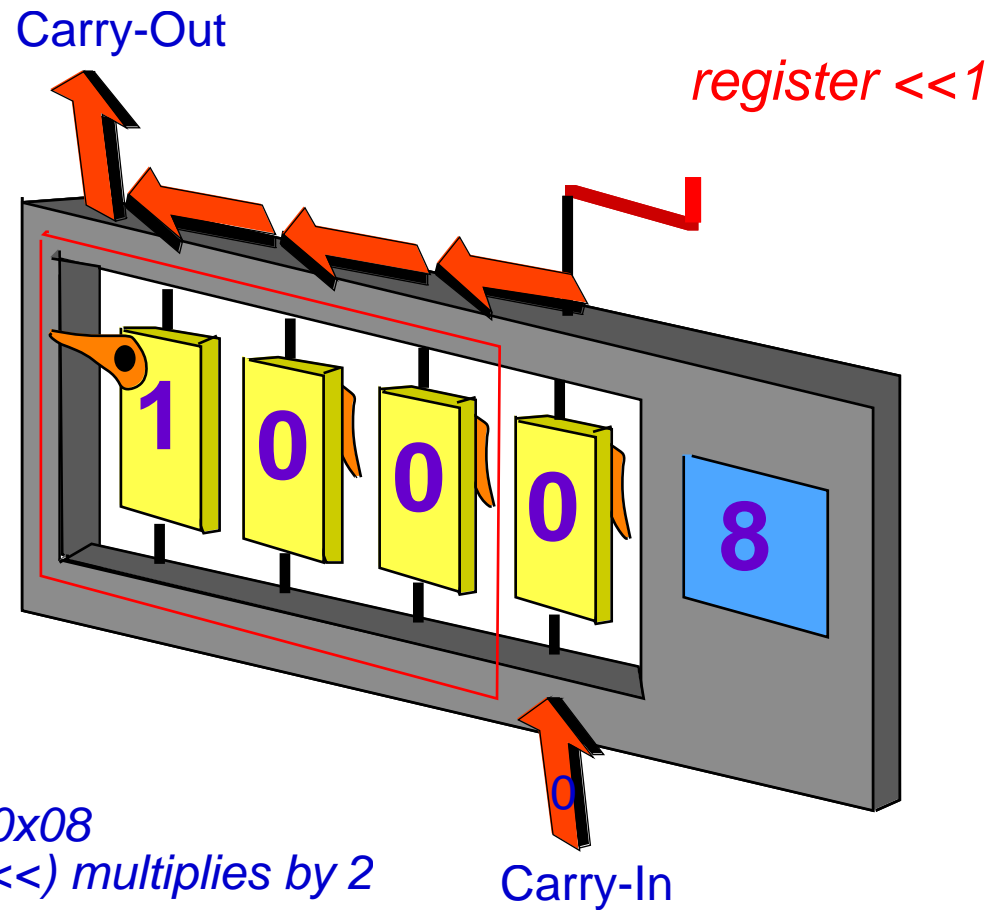
a shift right n places as `>>n`, meaning divide by  $2^n$

Hence `0x2>>1 = 0x1`, `0xF>>2 = 0x3`.

Use ***Booth's algorithm*** to perform long division

# Model Left Shift Register

Gorry Fairhurst

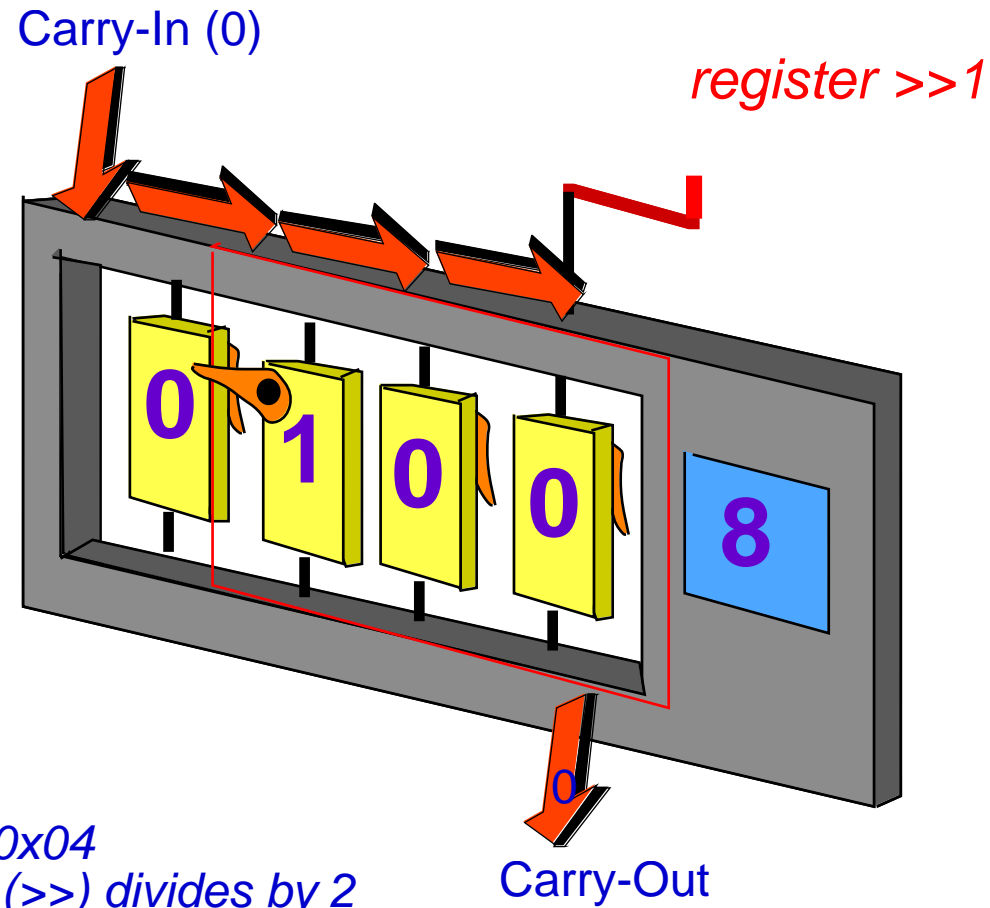


N.B.  
 $0x04 \ll 1 = 0x08$   
A shift left (<<) multiplies by 2



# Model Right Shift Register

Gorry Fairhurst



N.B.  
 $0x08 \gg 1 = 0x04$   
A shift right ( $\gg$ ) divides by 2

# 4-Bit Shift Register

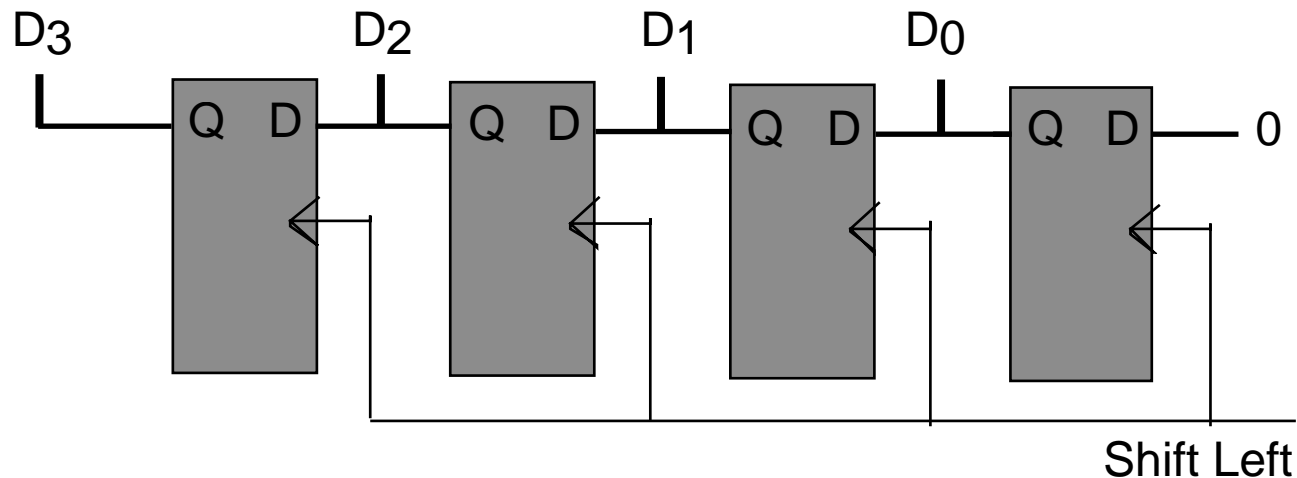
Gorry Fairhurst

Shifting is actually implemented by a shift register

The basic operation is the same:

Output of each bit feeds the input of the next

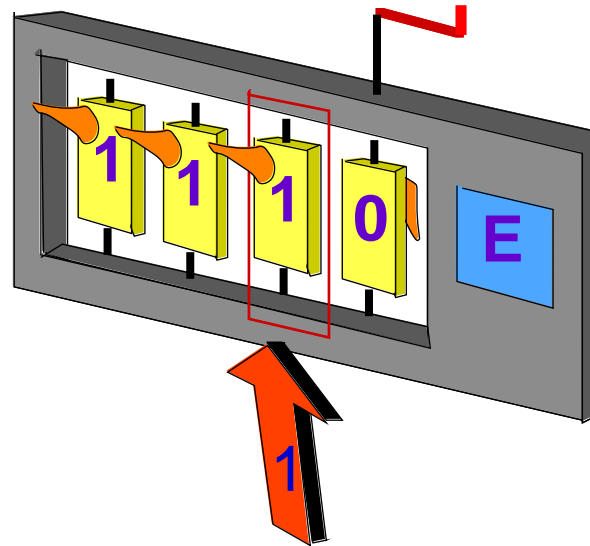
The last bit generates a “carry”



# Bit-Wise Logical Operators in the Model Register

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OR (preset)



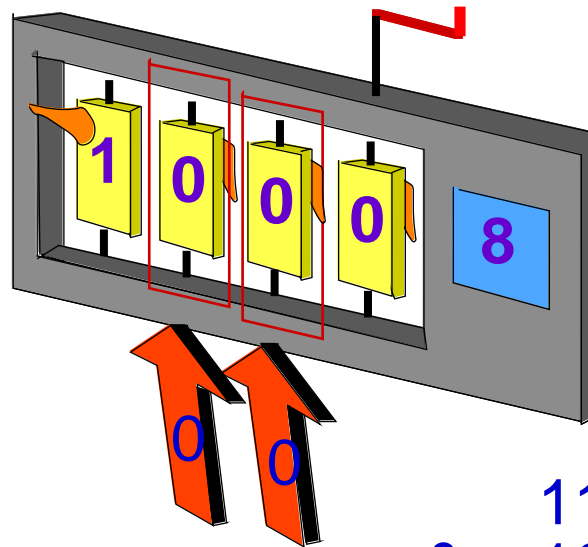
OR     1100  
=     0010  
      1110

N.B.    A OR 0 = A  
         A OR -1 = -1

# Bit-Wise Logical Operators in the Model Register

Gorry Fairhurst

*AND (clear)*



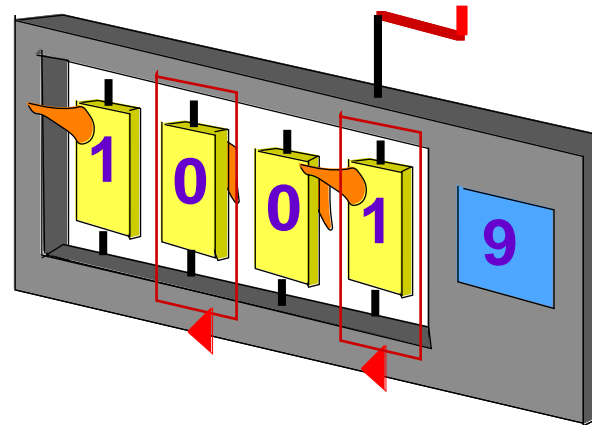
$$\begin{array}{r} 1100 \\ \& 1001 \\ = 1000 \end{array}$$

N.B.  $A \text{ AND } 0 = 0$   
 $A \text{ AND } -1 = A$

# *Bit-Wise Logical Operators in the Model Register*

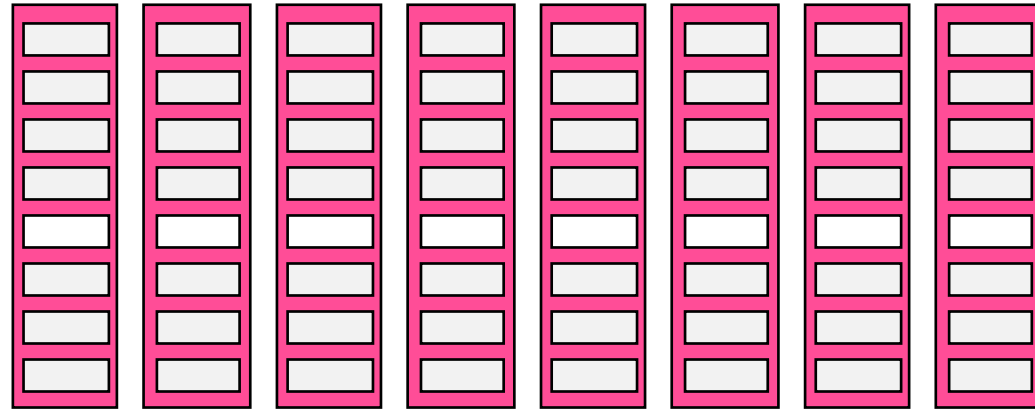
Gorry Fairhurst

*XOR (invert)*



1100  
XOR  
0101  
=  
1001

N.B.  $A \text{ XOR } -1 = \sim A$

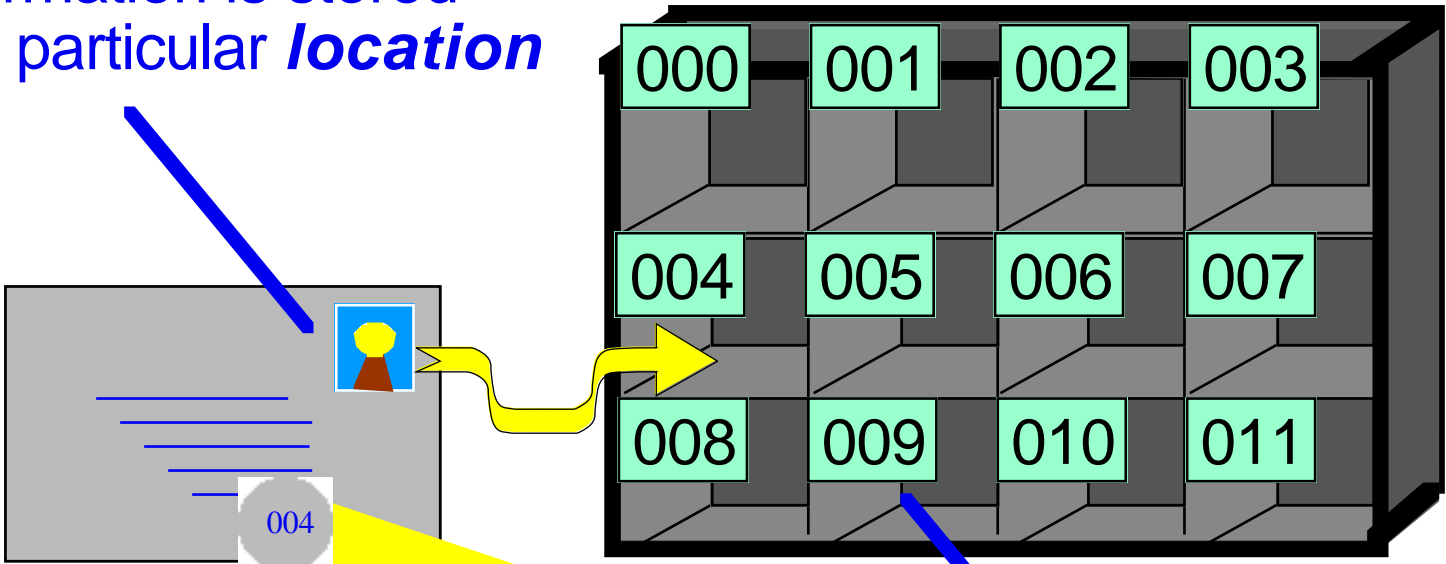


# Caches & Memory

# Storing Information in Memory

Gorry Fairhurst

Each piece of information is stored in a particular **location**



004

004

Every memory cell has a unique **address**

# Address and Values

Gorry Fairhurst

0	0
1	11
2	5
3	23
4	12
5	62

Address of byte

Value of byte  
(0...255)

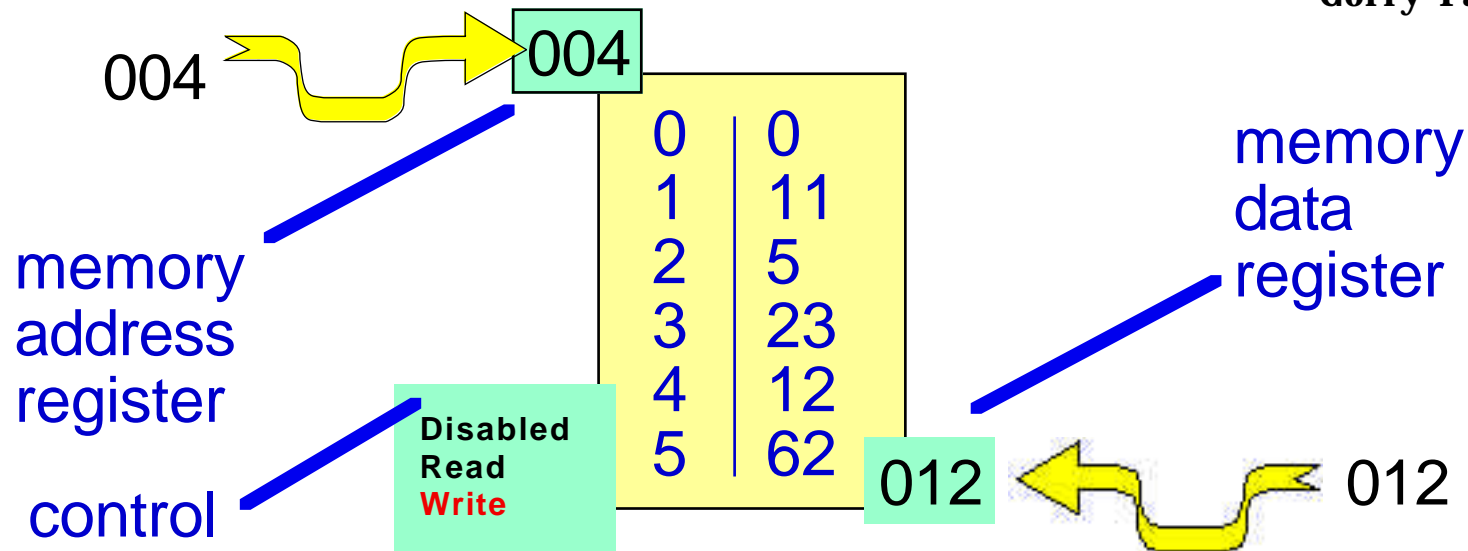
Memory is normally thought of as linear list  
(in computing we call this an **array**).

Memory locations normally store a single BYTE  
(each location stores a number 0..255)



## Writing a Value to an Address

Gorry Fairhurst

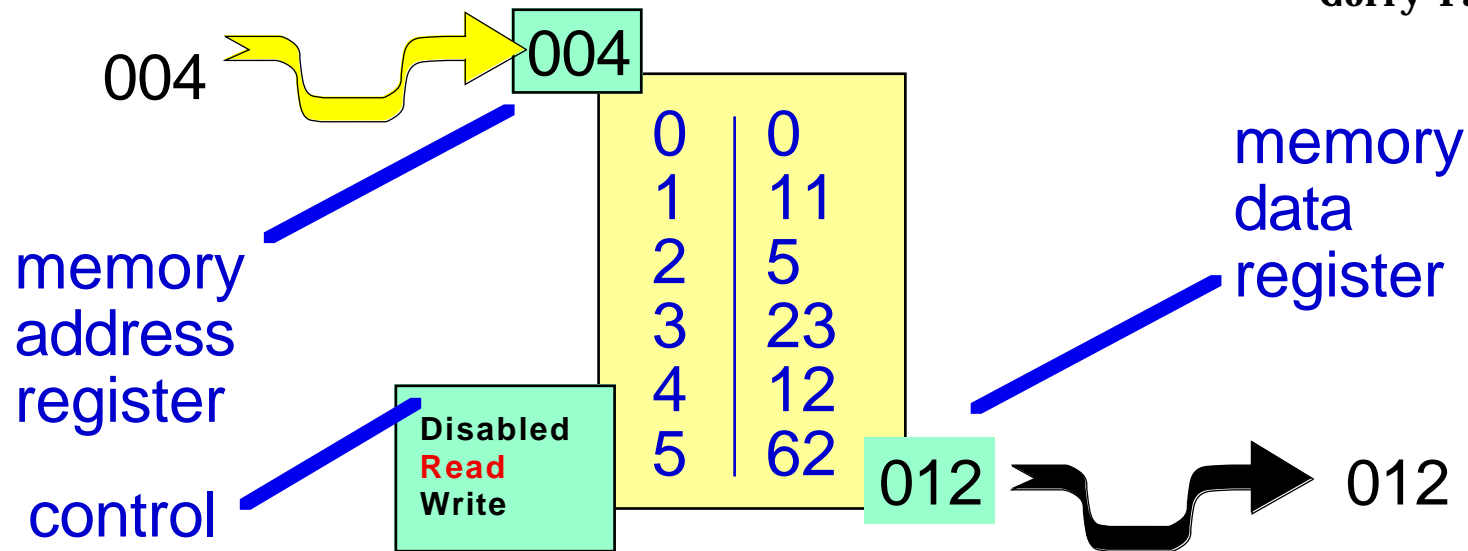


To write a value to the 4th location:

- (i) Set the memory address value to 4
- (ii) Set the data register to the value (e.g. 23)
- (iii) Activate the WRITE control
- (iv) DISABLE the memory

## Reading the Value at an Address

Gorry Fairhurst



To read a value from the 4th location:

- (i) Set the memory address value to 4
- (ii) Set the memory to READ
- (iii) The data register returns the value (e.g. 23)
- (iv) DISABLE the memory

# *Random Access Memory (RAM)*

---

Gorry Fairhurst

Read / Write supported

Used for storing programs and data

Looses all data when power removed (volatile)

Non-volatile alternatives:

ROM, EPROM, FLASH



# *Read Only Memory (ROM)*

---

Gorry Fairhurst

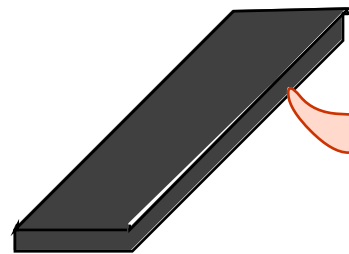
Program/Data is set at manufacture

May be mass-produced very cheaply

Can never be changed (except by replacing ROM)

Used for storing parts programs that never change  
e.g. parts of operating system kernel (firmware)

For programs it is more flexible to use EPROM, FLASH



There is no  
write control!

# Flash Memory

---

Gorry Fairhurst

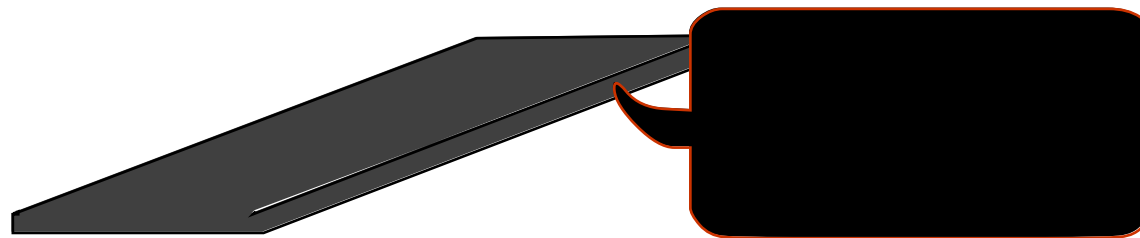
Program/Data is written by CPU

May be upgraded very easily

Used primarily for storing programs  
and configuration data

Very expensive compared to ROM, EPROM

Much slower (particularly to write) than RAM



# *Erasable Programmable Read Only Memory*

---

Gorry Fairhurst

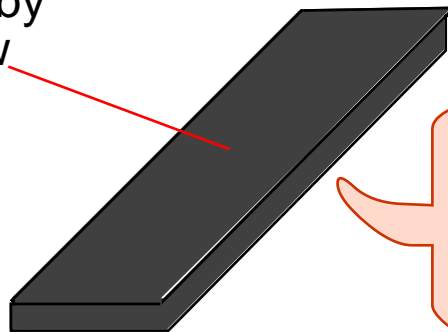
Program/Data is written by an EPROM programmer

Whole chip needs to be erased  
(needs to be taken out of computer)

Used primarily for storing programs

More expensive than ROM, but reusable

EPROM erased by  
exposing window  
to Ultra-Violet  
Light



Erase, write,  
read many times

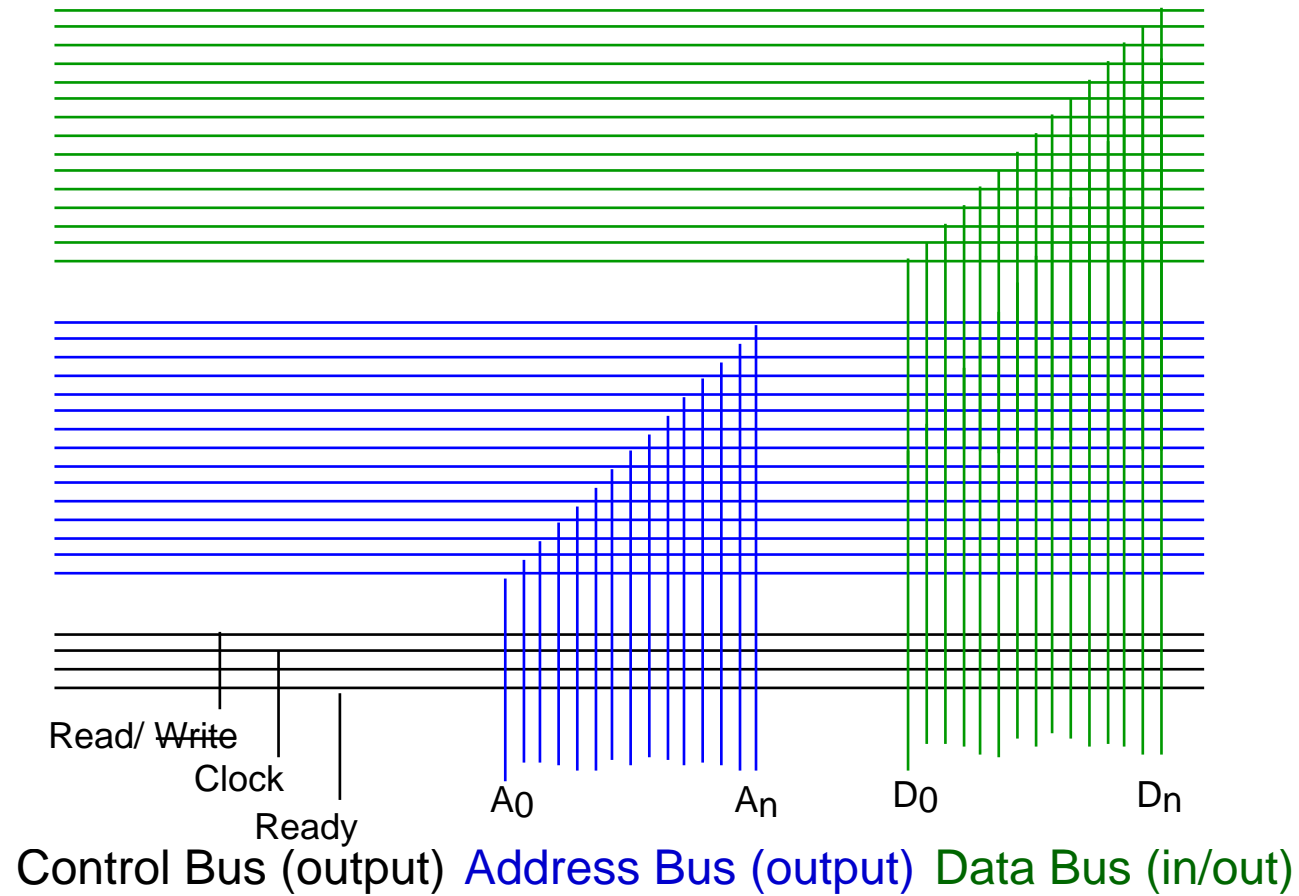
# Memory

Gorry Fairhurst

<b>Volatile memory</b> (loses data when no power)		<b>Non-volatile memory</b> (keeps data when no power)		
Dynamic RAM (cheap)	Static RAM (expensive)	ROM (cheap)	EPROM (cheap)	FLASH (cheap)
fast	very fast	fast	fast	slow
main memory	cache & I/O buffer	programs (one use)	programs (reusable)	programs and data

# Address, Data, & Control Bus

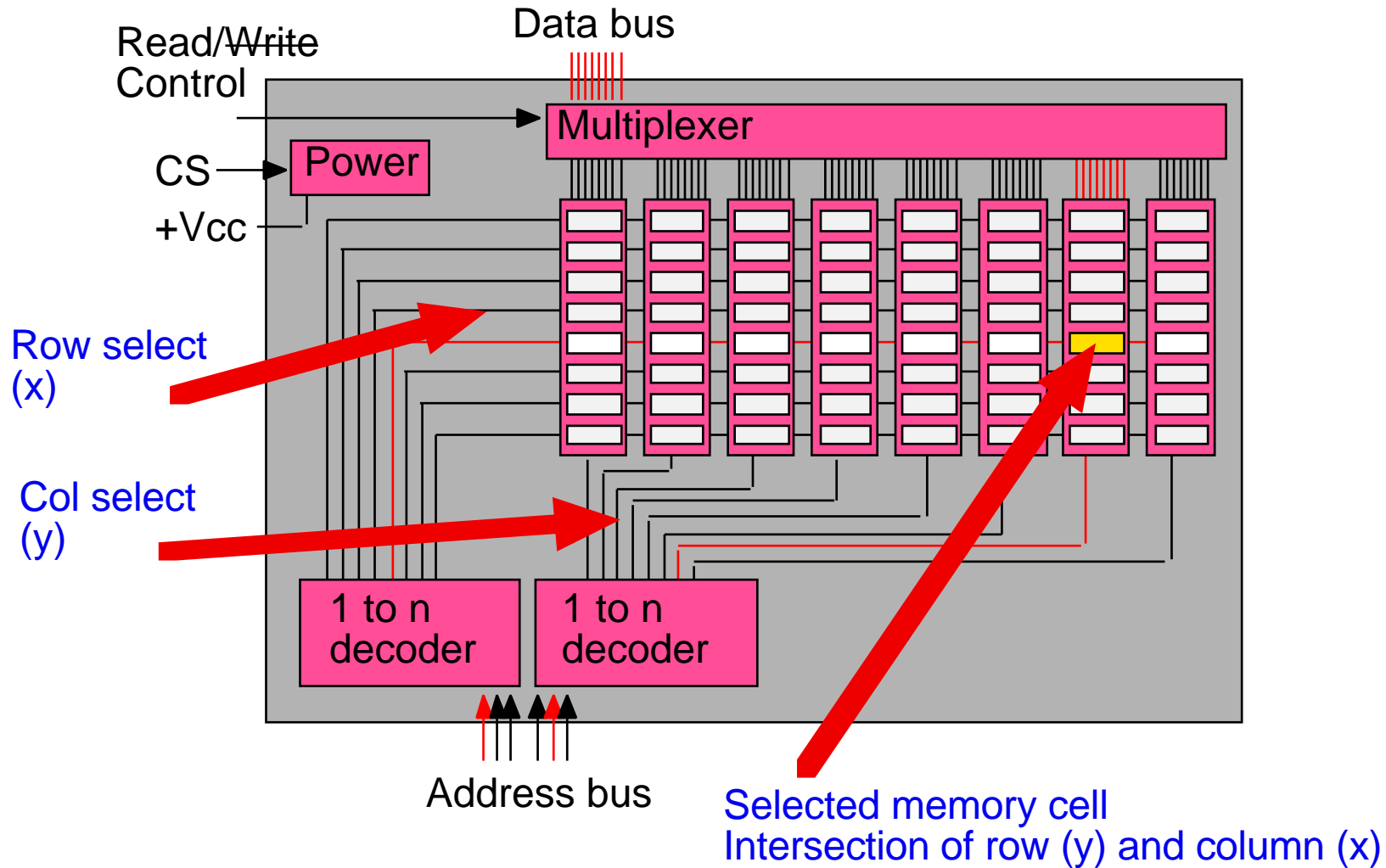
Gorry Fairhurst





# Random Access Memory (RAM)

Gorry Fairhurst



# Decoder

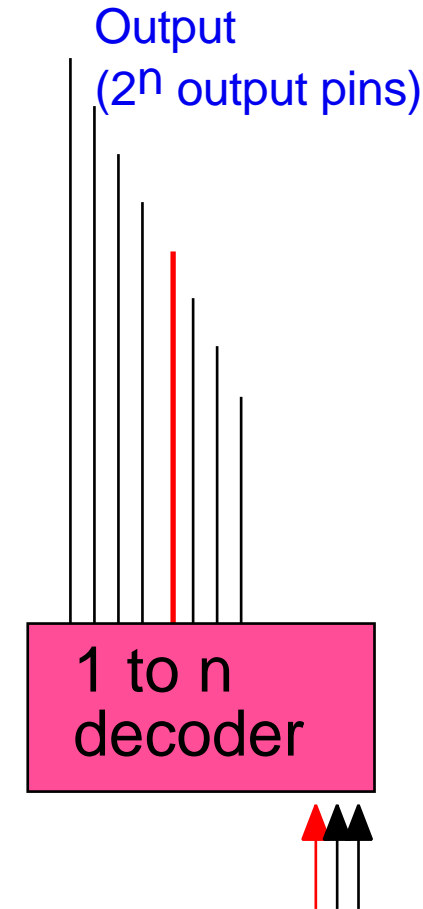
Gorry Fairhurst

The decoder selects only one output pin

Hence a 3 bit decoder selects 1 of 8 pins

An input of 100 (4)  
places a 1 at the output pin 4  
and a 0 at all other output pins.

An input of 101 (5)  
places a 1 at the output pin 5  
and a 0 at all other output pins.



Dec.	Binary
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111

## Chip Select (CS)

Gorry Fairhurst

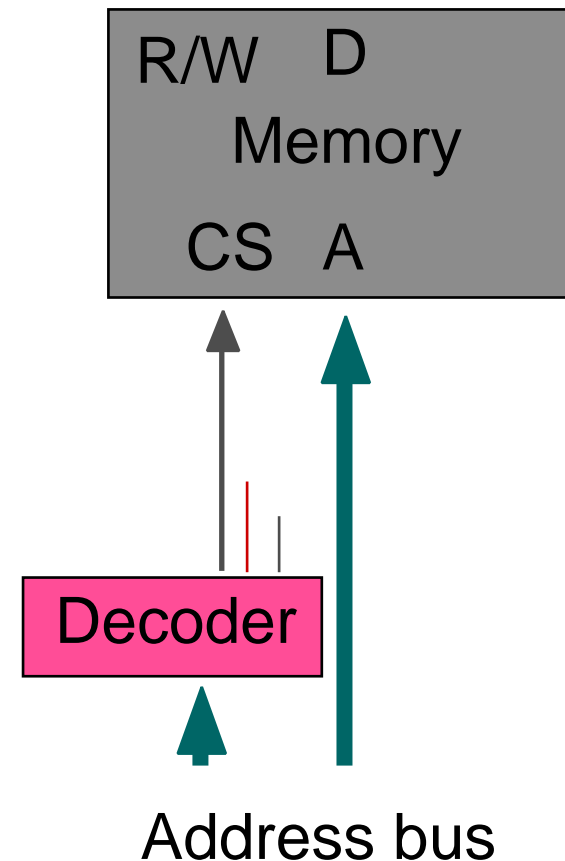
Control input that enables the chip

- if CS=0, ignores all other pins
- if CS=1, obeys R/W controls.

At any time, only one chip has CS=1, others must have CS=0.

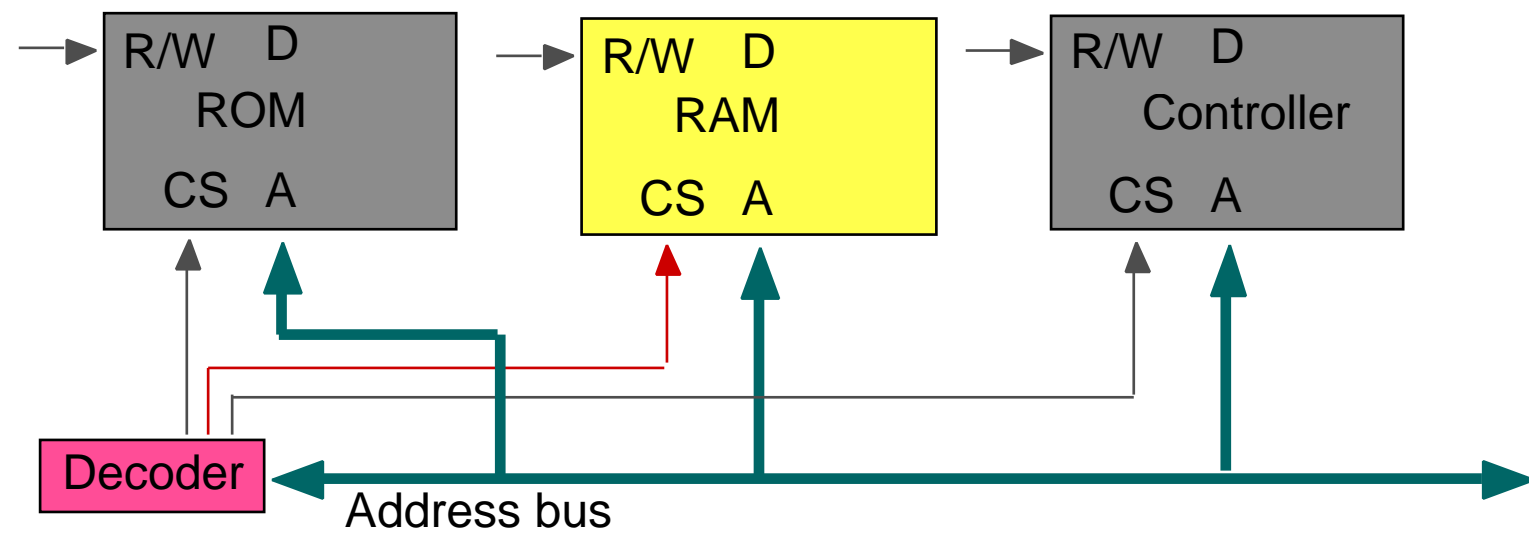
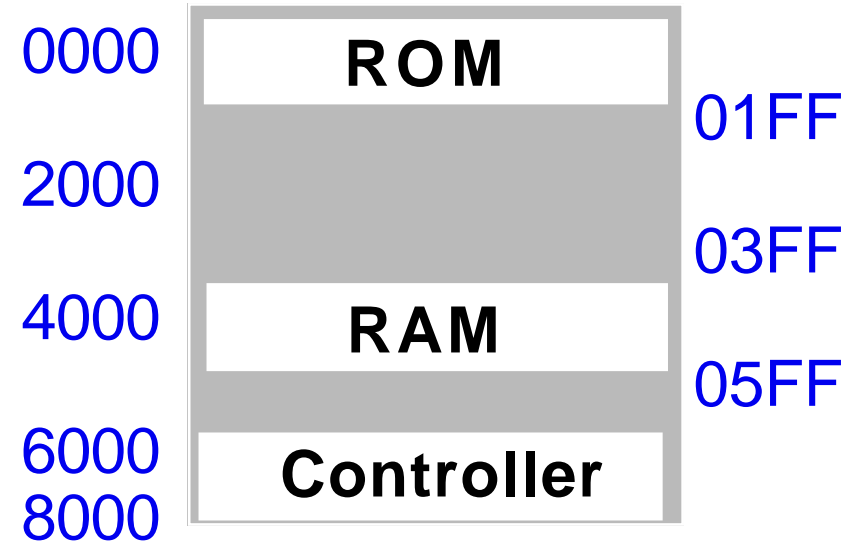
CS value obtained by feeding highest bits of address bus to a decoder. Each CS is connected to an output.

The lower bits of the address bus connect to address pins of the chip.



# Memory Map

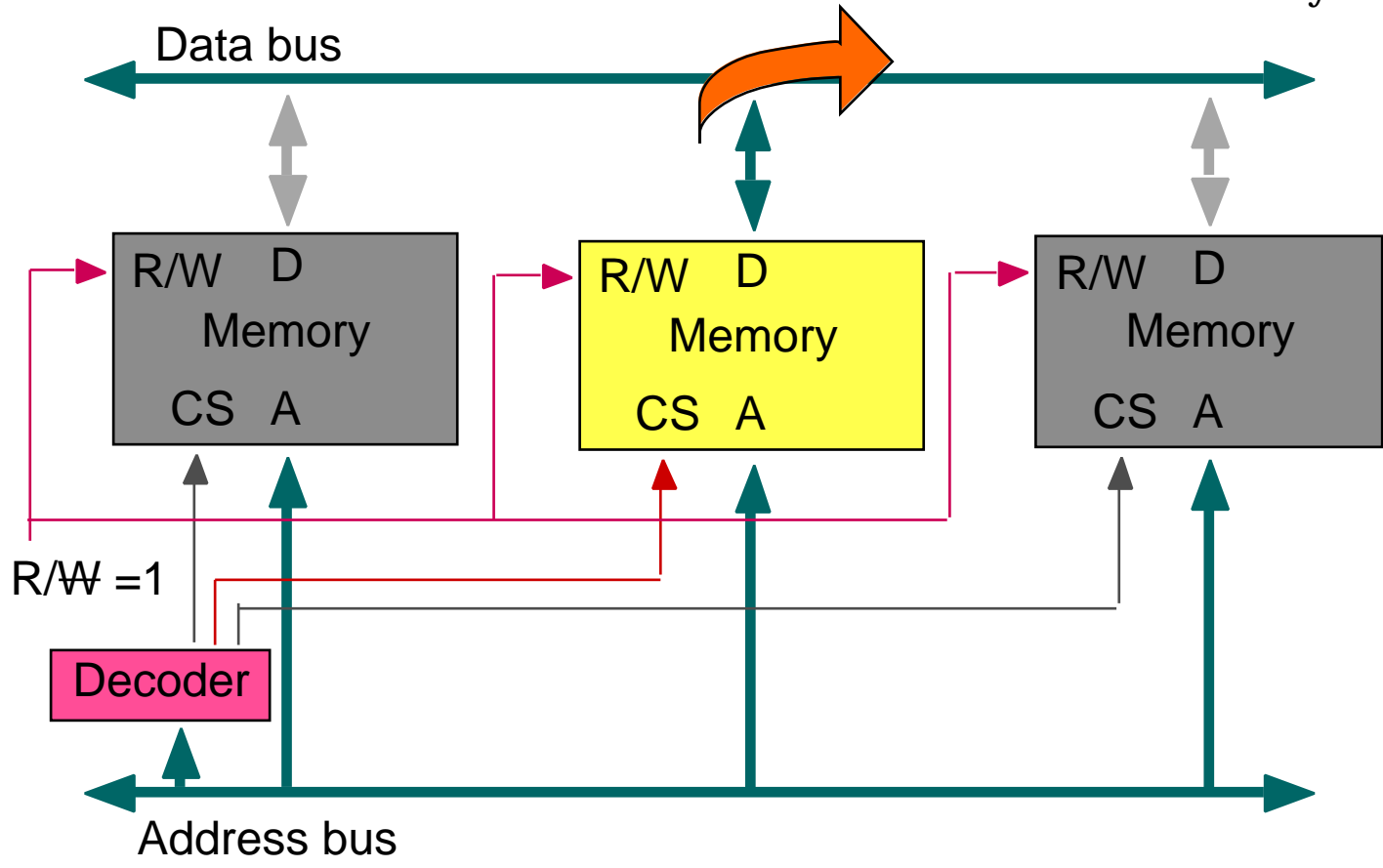
Gorry Fairhurst





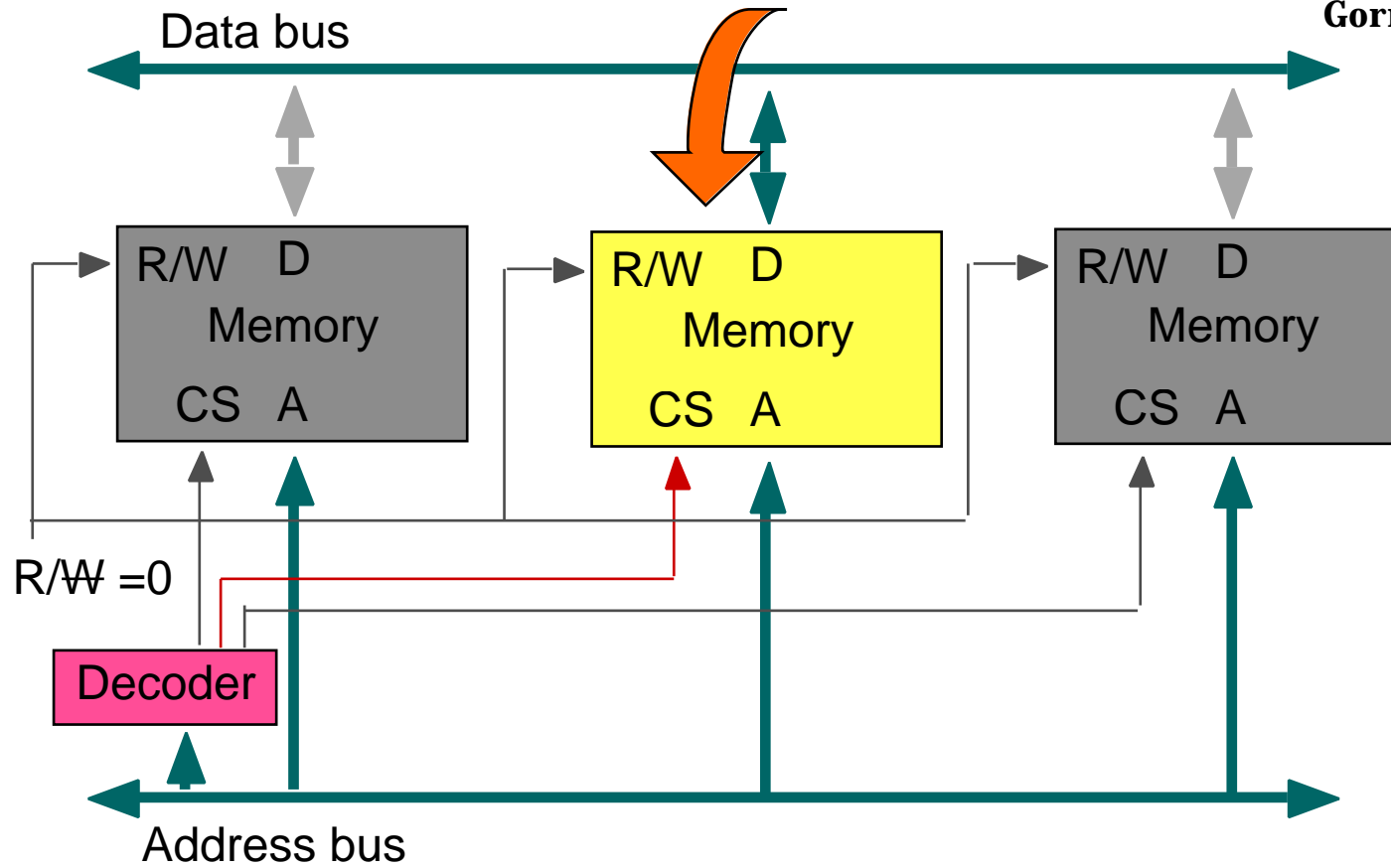
# Reading a Location in Memory

Gorry Fairhurst



# Writing a Location in Memory

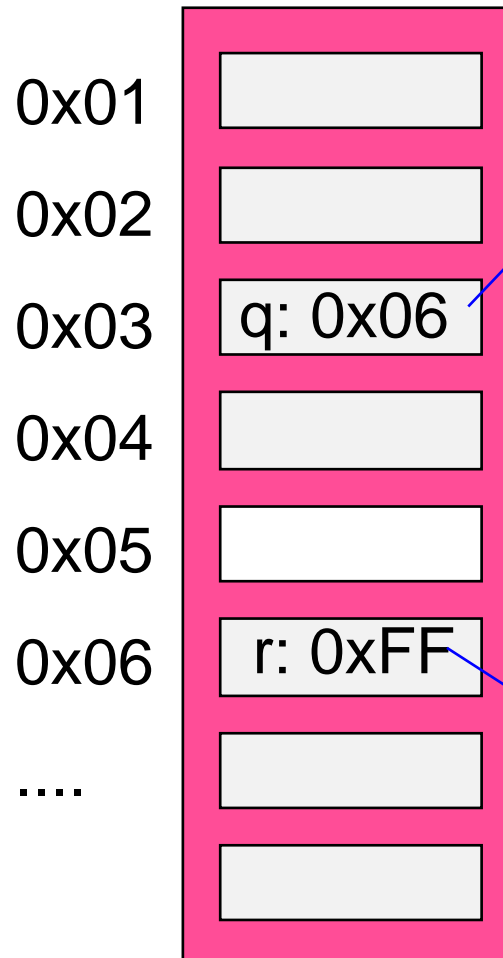
Gorry Fairhurst



# Addresses and Memory

Gorry Fairhurst

Addresses



a variable labelled "q"

The value of q:  
`q == 0x06`

The address of q:  
`&q == 0x03`

q used as a pointer:  
`*q == r == 0x06`  
(in assembler `*q==(q)`)

a variable labelled "r"  
`r == 0xFF`  
`&r == 0x06`

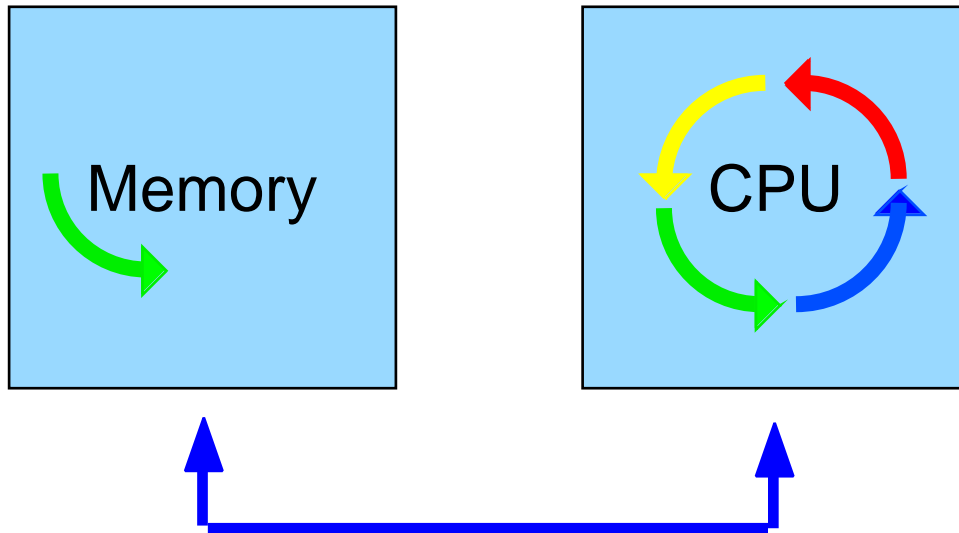


# *CPU's are faster than Memory*

---

Gorry Fairhurst

CPU's operate *much* faster than memory does!



Accessing memory is a severe *bottleneck*

# Accessing Memory

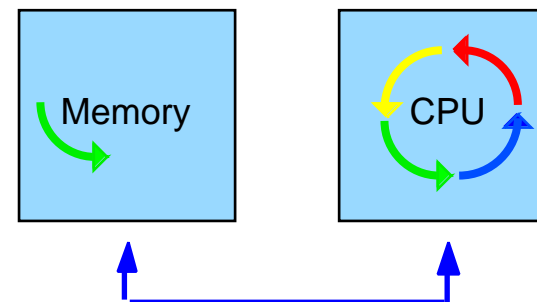
Gorry Fairhurst

Three fortunate observations:

Programs may be optimised  
Using registers instead of memory to reduce **data** transfer

Programs often execute loops of instructions  
The same **instructions** are often used many times

Programs usually read and write consecutive locations  
**Data** are often stored in words, or larger groups of bytes



# Caches

Gorry Fairhurst

Caches can do three things to improve performance:

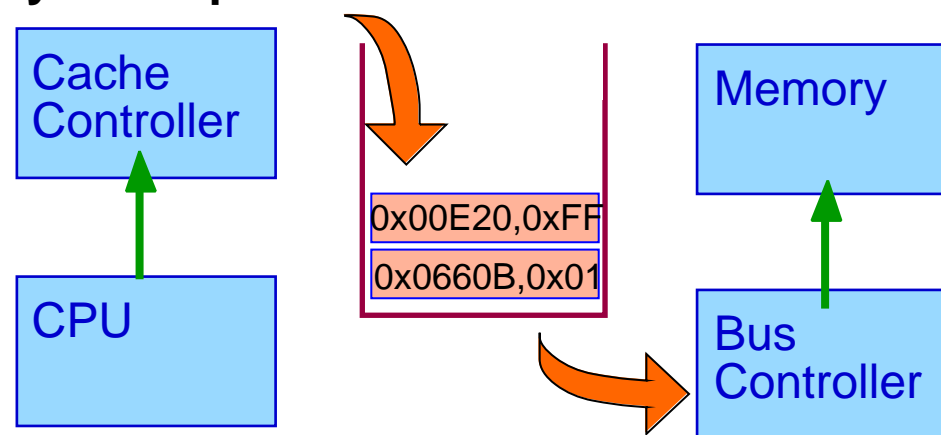
Recently **read** data kept in fast memory for quick re-use

They **read** locations from memory before they are required

They defer **writing** data to memory

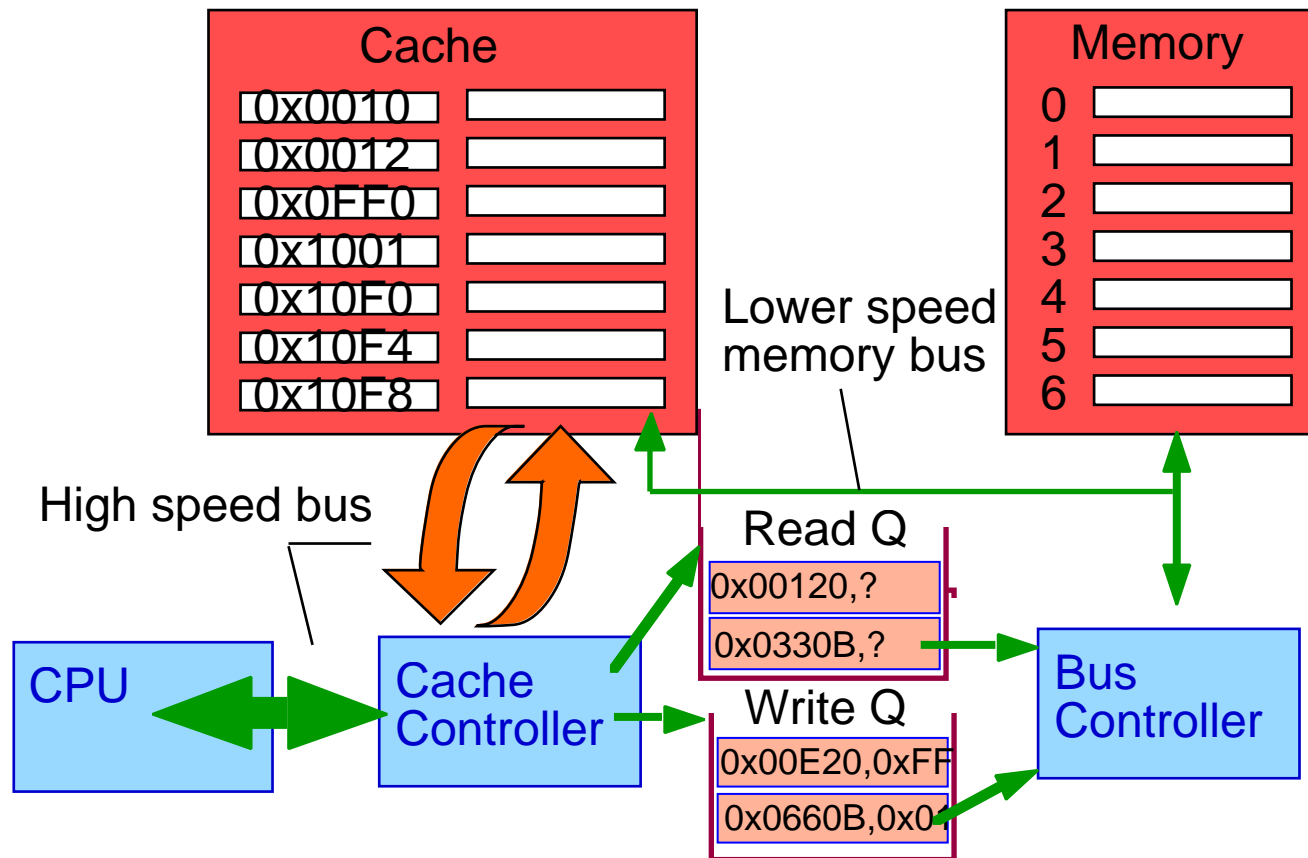
Allowing program to continue while memory catches up

## The memory write queue



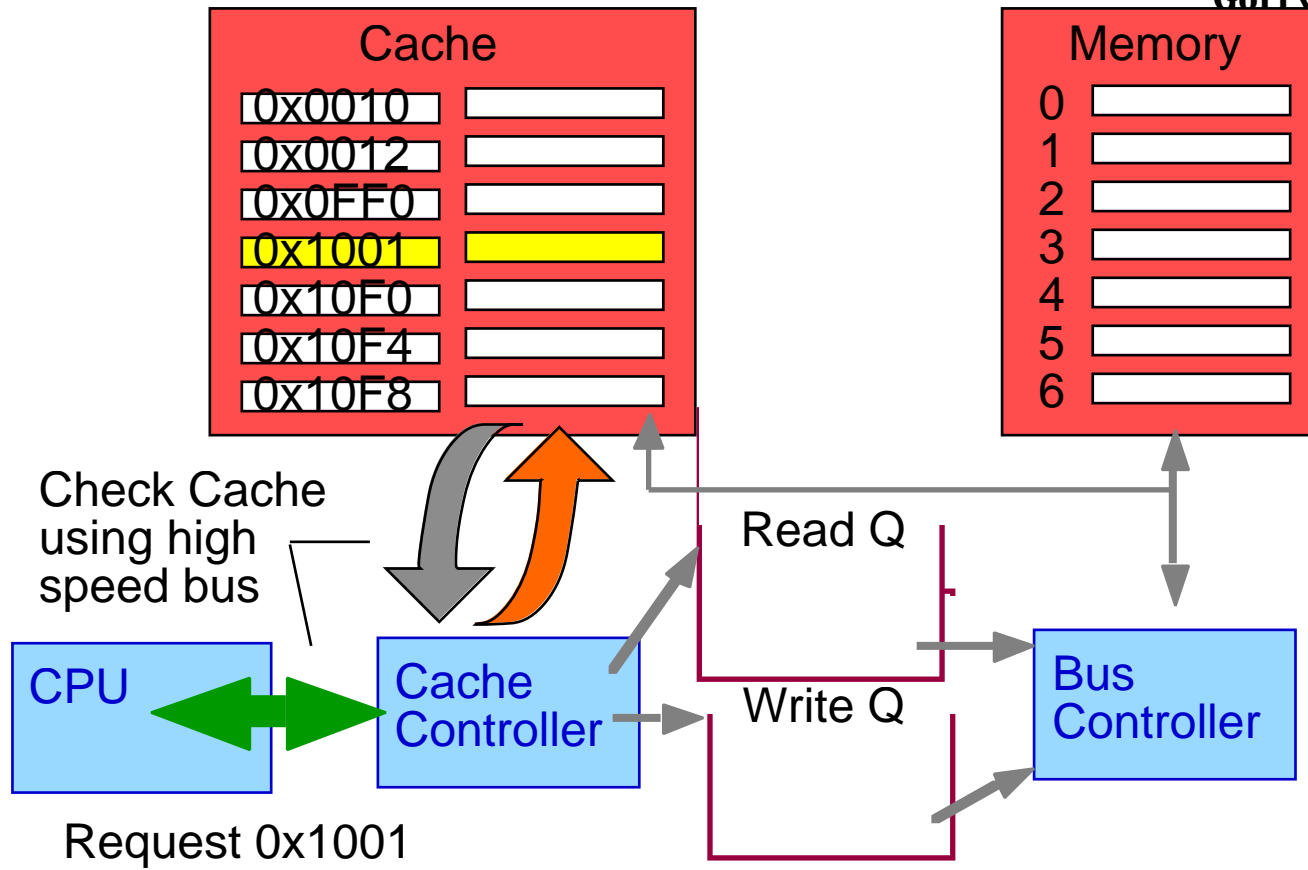
# Cache

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# Read from Memory (in Cache)

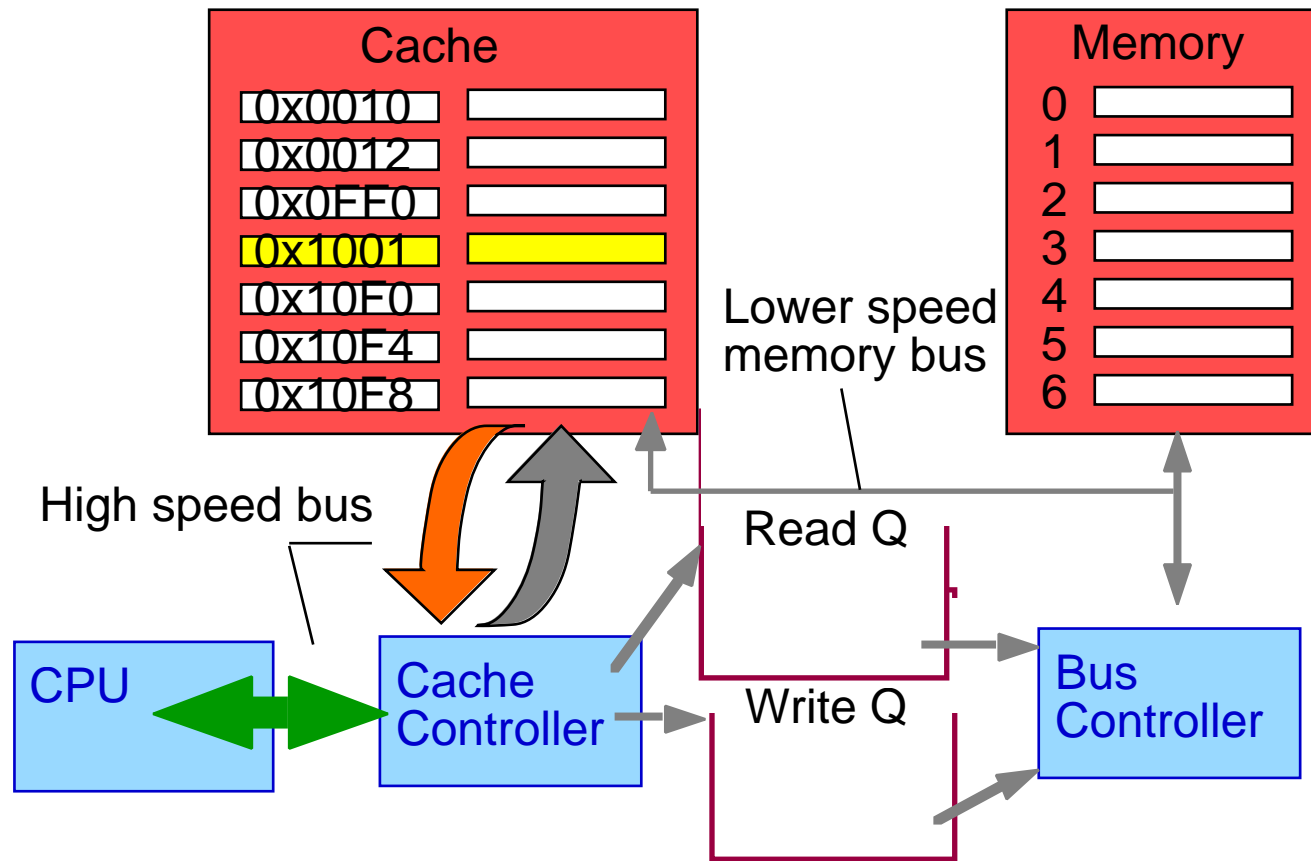
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*Part 1: Before looking at RAM,  
check the locations stored in the Cache*

# Read from Memory (in Cache)

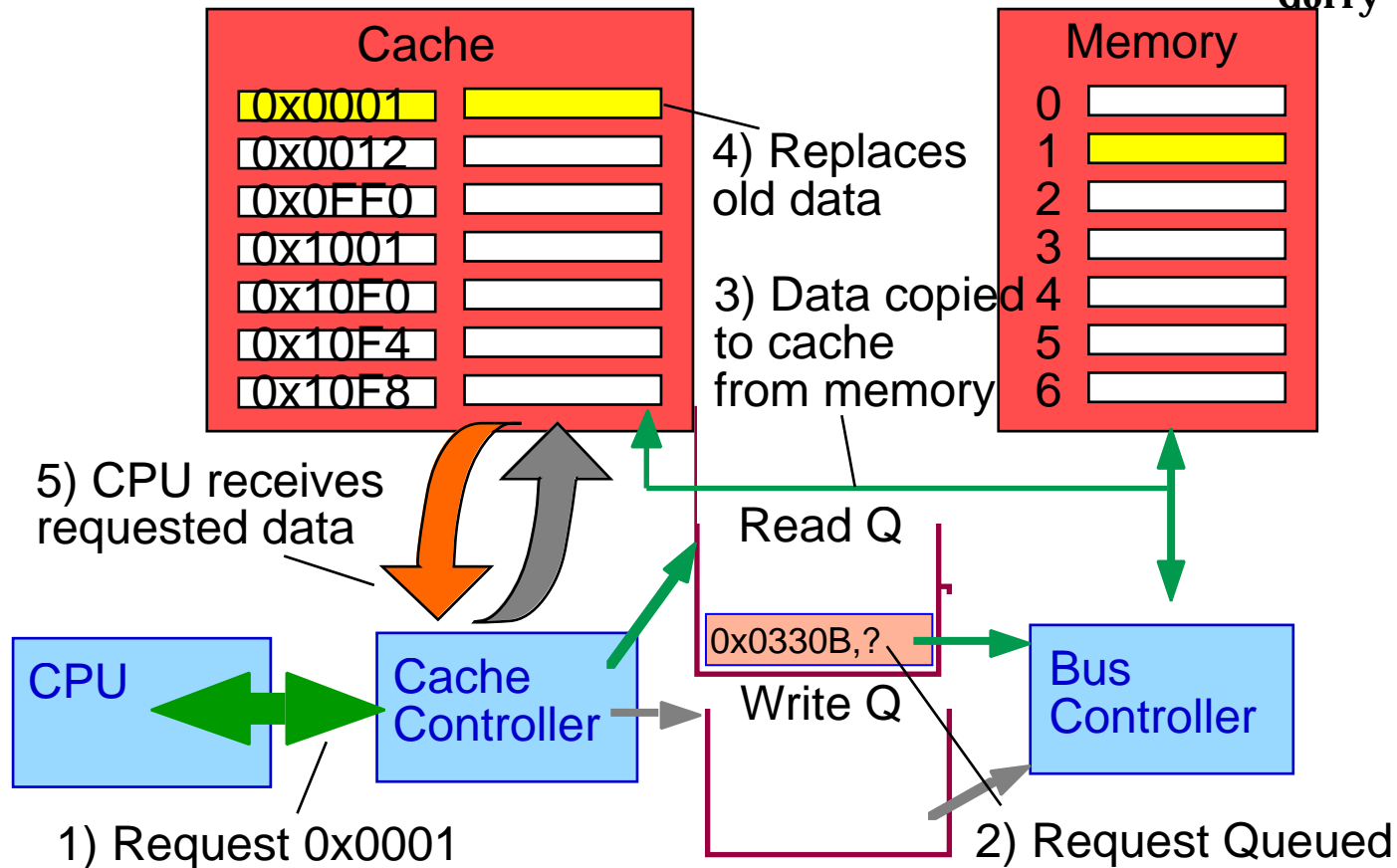
Gorry Fairhurst



*Part 2: If the location is in the Cache, use the value stored in the Cache*

# Read from Memory (Not in Cache)

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*Part 2: If the location is NOT in the Cache, fetch value from RAM (also store in Cache)*